

*Characterization of Micropore Structure of Porous Materials  
Using DFT Models Applied to Ar, N<sub>2</sub> and H<sub>2</sub> Adsorption Data.*

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# Outline of the presentation

- Objective
- Earlier results
- Experimental
- Assumptions of model calculations
- Method of the PSD calculation
- Calculation of carbon PSDs using multiple adsorbates: Examples
- Fundamental and practical advantages of using more than one adsorbate for PSD analysis
- DFT based prediction of high-pressure H<sub>2</sub> adsorption at ambient temperature from H<sub>2</sub> measurements at 77 K
- PSD analysis for zeolites
  - Effect of pore sizes and materials chemistry
- Conclusions

# Objective

Discussion of the micropore structure analysis of porous  
{nanoporous, microporous}  
materials based on adsorption measurements of standard  
adsorbates N<sub>2</sub> and Ar, and H<sub>2</sub> isotherms  
at cryogenic temperatures .

# Earlier results

## Comparison of PSDs calculated from different adsorbates

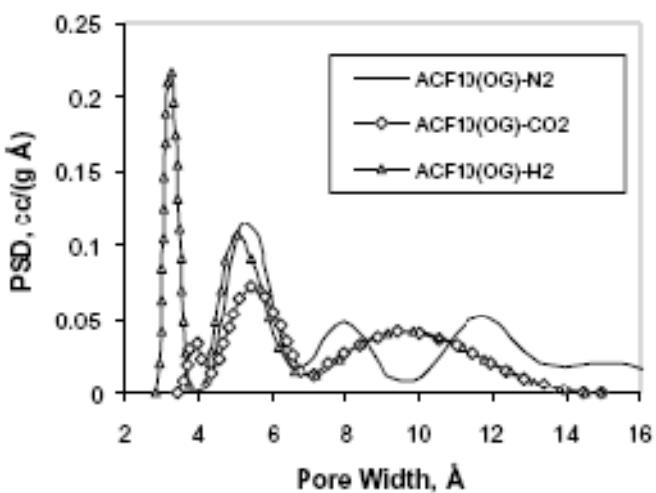


Fig. 6. Differential PSDs calculated from H<sub>2</sub>, N<sub>2</sub>, and CO<sub>2</sub> isotherms for the ACF10(OG) sample.

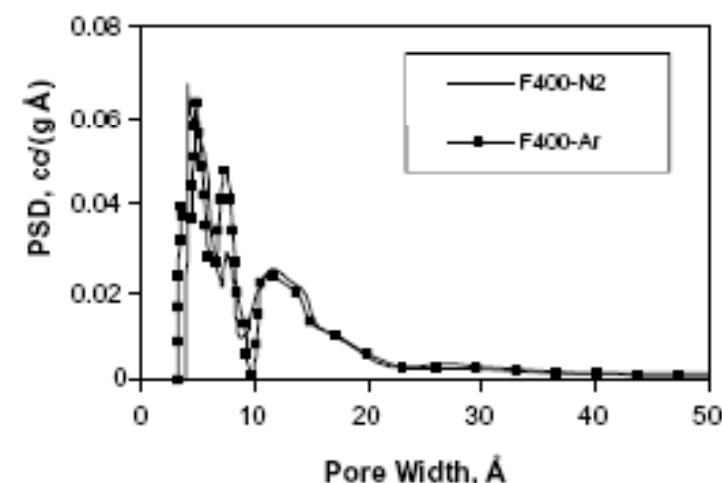


Fig. 4. PSDs of coal based activated carbon F400 obtained from the DFT analysis of N<sub>2</sub> and Ar isotherms at 77 K.

J. Jagiello, M. Thommes, Carbon Conference, Oviedo (2003)  
Carbon 42,1227–1232 (2004)

# Earlier results

## $H_2$ Adsorption on Takeda 3A Carbon Molecular Sieve

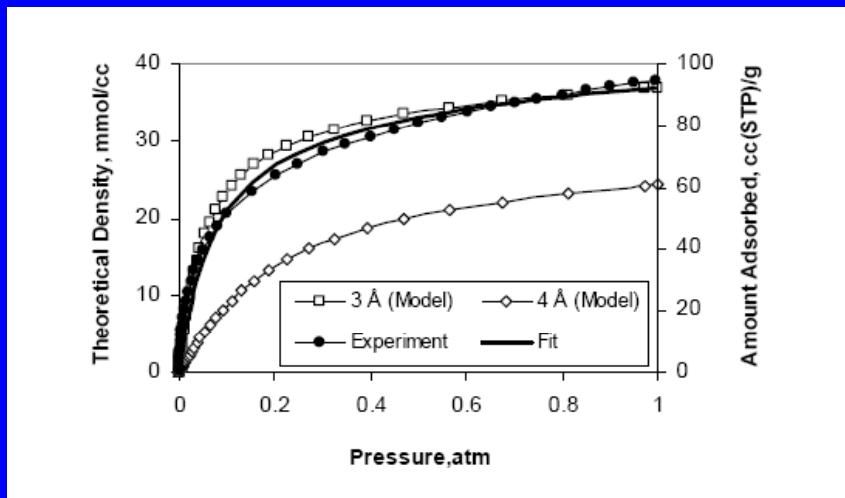


Figure 1. Experimental H<sub>2</sub> isotherm measured at 87 K for the Takeda 3A sample compared with the NLDFT isotherms calculated for the 3 and 4 Å pores and with the curve fitted by SAIEUS.

Jagiello, J.; Thommes M.; Linares-Solano, A.; Cazorla-Amorós, D.; Lozano-Castelló, D., Extended Abstracts, Carbon 2004

# Experimental

## Materials

### Set 1:

Carbons derived from poly(ethylene terephthalate), PET

Sample PC obtained by pyrolysis of PET.

Samples PC12, PC35, PC58, and PC76 obtained from PC by CO<sub>2</sub> activation with increasing burn-off (12, 35, 58, 76 %)

Details: Parra JB, Ania CO, Arenillas A, Rubiera F, Palacios JM, Pis JJ., J Alloys Compd, 379: 280–89 (2004)

### Set 2:

Commercial CMSs from Supelco obtained from polymeric precursors

Details: Jagiello, J., Betz, W. Microporous and Mesoporous Materials, **108**, 117–122 (2008)

Sample ACF10, Activated carbon fiber (Kynol)

Details: Jagiello, J., Thommes, M. Carbon 42,1227–1232 (2004)

Commercial Zeolite Samples (Aldrich)

# Outline of model calculations

- Model **NLDFT** isotherms (kernels) are calculated using **Tarazona** approach [1, 2].
- **Slit pore model** for carbon pores.
- Carbon-gas interactions described by the **Steele potential** [3].
- LJ parameters for N<sub>2</sub> and Ar taken from **Ravikovitch** et al. [4].
- **Weeks-Chandler-Andersen** attractive potential [2].
- H<sub>2</sub>-H<sub>2</sub> interactions: **Silvera-Goldman** [5] potential modeled by LJ potential [6]  
 $e_{ff}/k = 34.3 \text{ K}$ ,  $s_{ff} = 3.04 \text{ \AA}$
- Gas-solid interaction parameters for H<sub>2</sub>-carbon derived from the fit to experimental isotherm measured on graphitized carbon black [7]
- Quantum corrections for H<sub>2</sub> model applied by using **Feynman** “Effective Potential.”
- The **cylindrical** pore model is assumed for zeolite pores.

- 
1. Tarazona P, Marini Bettolo Marconi U, Evans R. *Mol Phys* 1987;60:573.
  2. Lastoskie C, Gubbins KE, Quirke N. *J Phys Chem* 1993;97:4786-96.
  3. Steele WA. *The Interactions of Gases with Solid Surfaces* Pergamon, Oxford, 1974.
  4. Ravikovitch PI, Vishnyakov A, Russo R, Neimark AV. *Langmuir* 2000;16:2311-2320.
  5. Silvera IF, Goldman VV. *J Chem Phys* 1978; 69: 4209
  6. Stan G, Cole MW. *J. Low Temp. Phys.* 1998; 110:539-544.
  7. J. Jagiello, A. Anson, M.T. Martinez, *J. Phys. Chem.*, 110 (2006) 4531

# Outline of the PSD calculation method

**Multi Adsorbate Integral Equation [1]:**

$$\min \sum_m^M \sum_i^{N_m} \left[ V_m(p_i) - \int_{\alpha_m}^{\beta_m} K_m(p_i, w) f(w) dw \right]^2 \quad (1)$$

$p_i$  - experimental pressure of i-th adsorption point

$V_m$  - measured adsorption isotherm for m-th adsorbate

$K_m$  - set of theoretical DFT isotherms (Kernel) for m-th adsorbate model

$f(w)$  - PSD

$w$  - effective pore width

$M$  - number of adsorbates/models

$N_m$  - number of points of m-th experimental isotherm

$f(w)$  is obtained by conditional minimization of (1) using regularization,  
SAIEUS [2], nonnegativity constraints [3], L-curve [4].

[1] Jagiello, J.; Thommes M.; Linares-Solano, A.; Cazorla-Amorós, D.; Lozano-Castelló, D., Extended Abstract, Carbon 2004

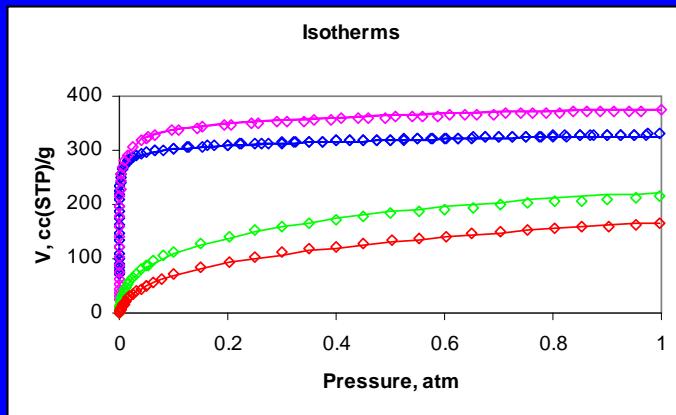
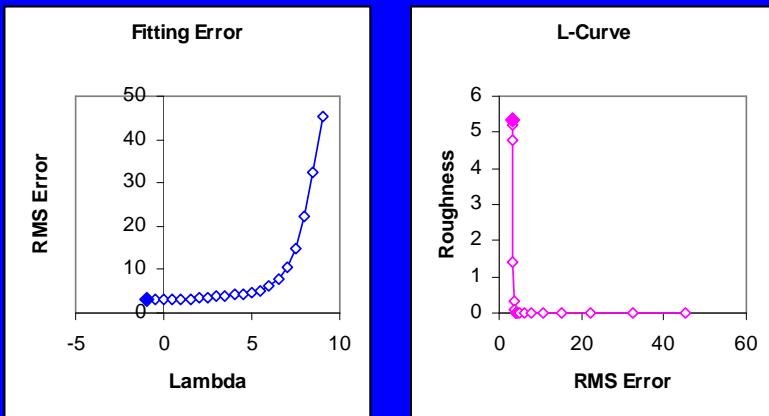
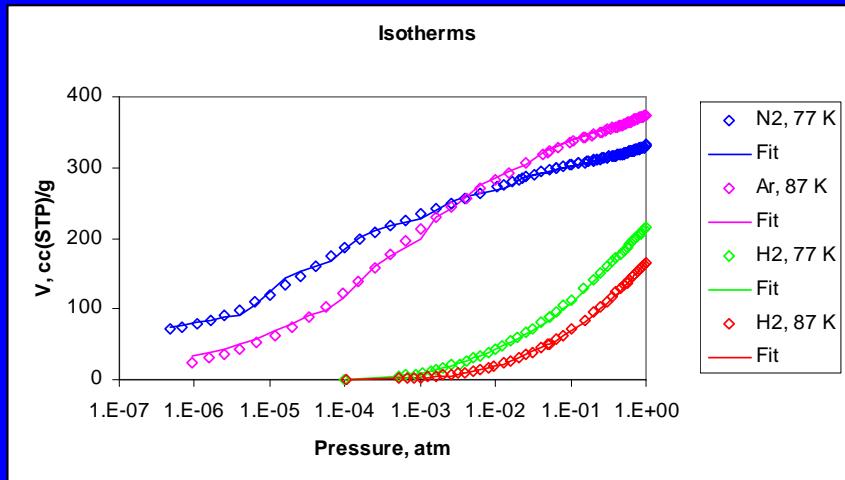
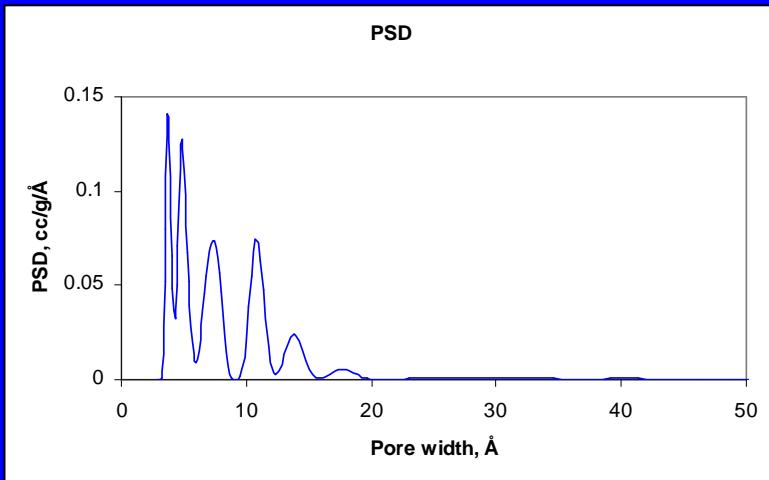
[2] Jagiello, J. Langmuir 1994, 10, 2778

[3] Lawson, C. L.; Hanson, R. J. Solving Least Squares Problems; Prentice-Hall: Englewood Cliffs, New Jersey, 1974

[4] Hansen, P. C.; O'Leary, D. P. SIAM J. Sci. Comput. 1993, 14, 1487

# Effect of regularization

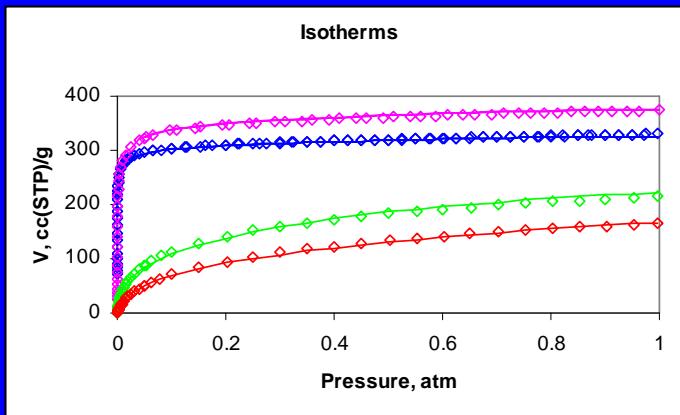
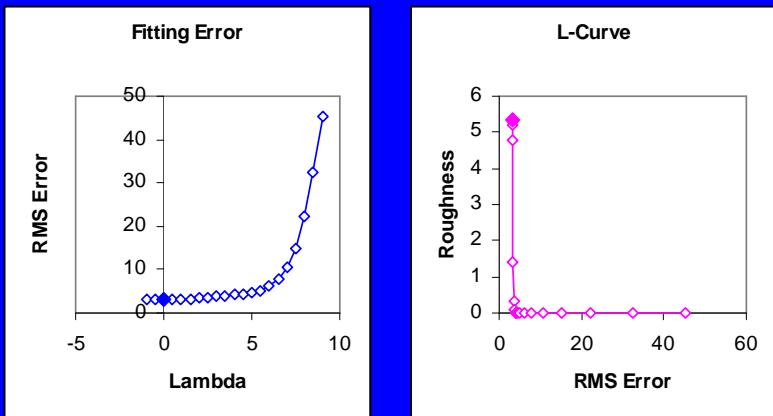
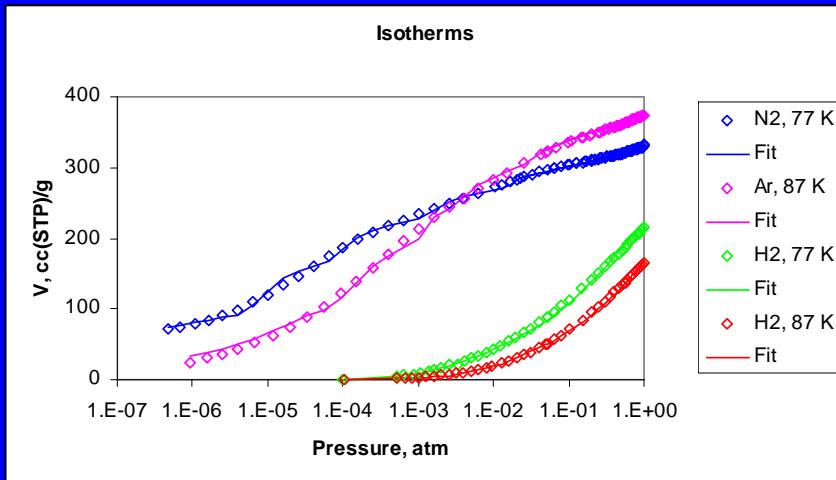
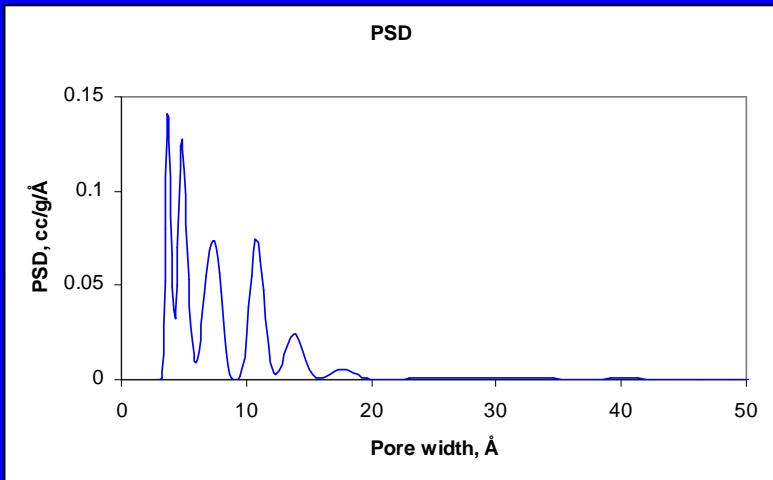
$$\lambda = -1$$



J. T. Duda, L. Jagiello, J. Jagiello, J. Milewska-Duda, Appl. Surface Sci., **253**, 5616–5621 (2007)

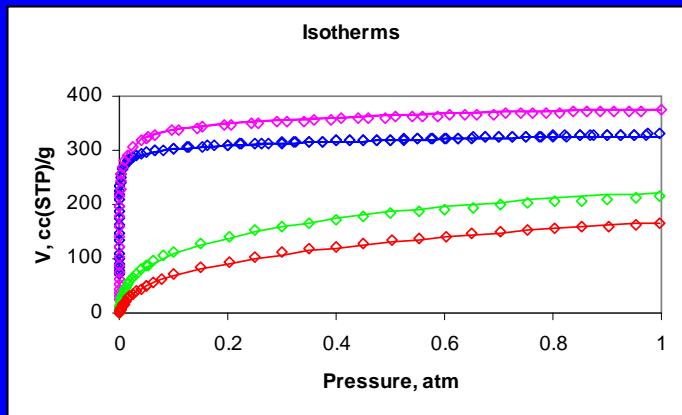
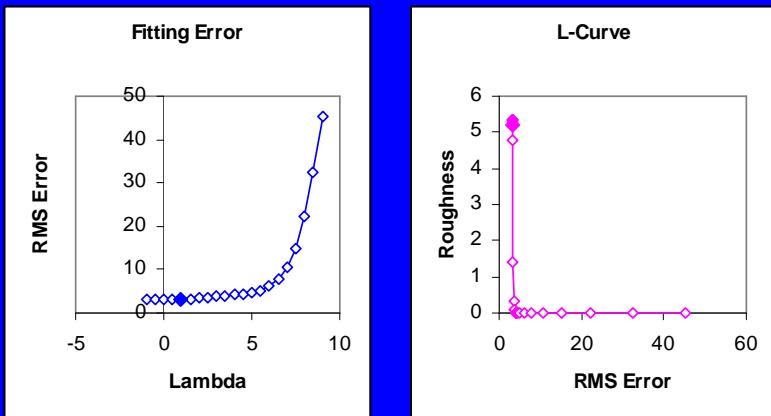
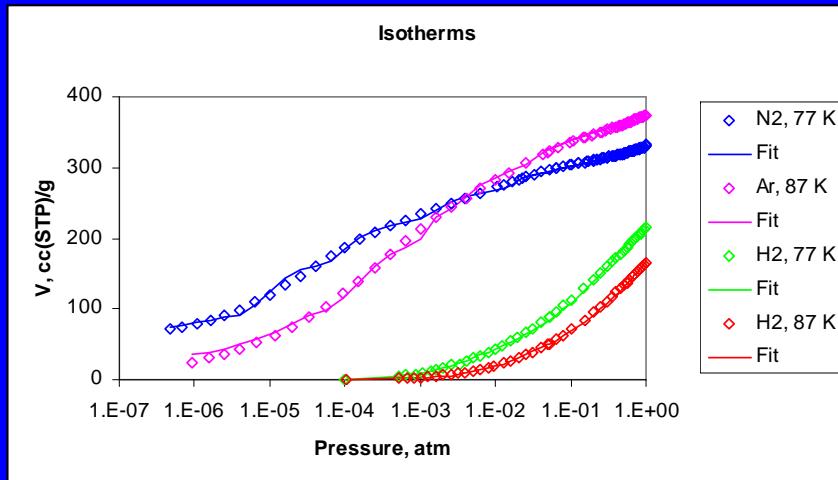
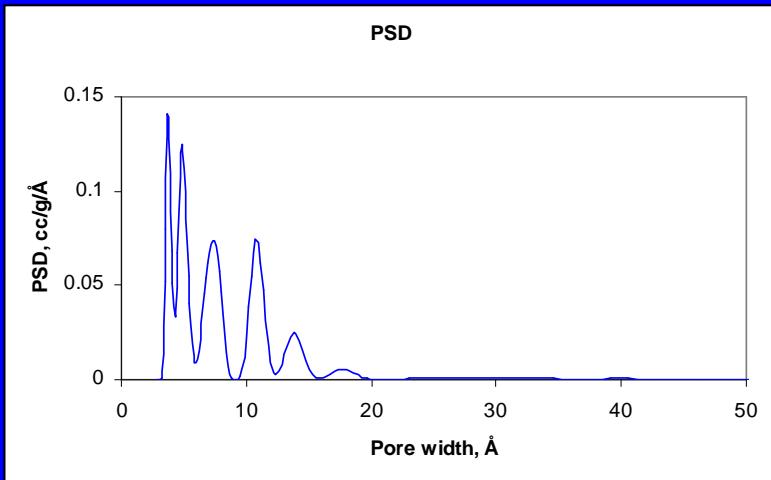
# Effect of regularization

$$\lambda = 0$$



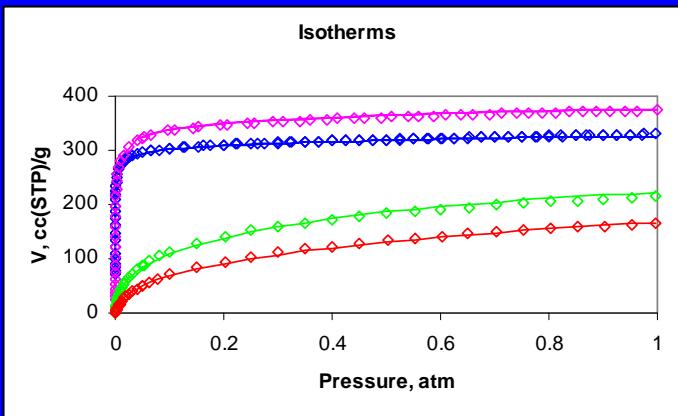
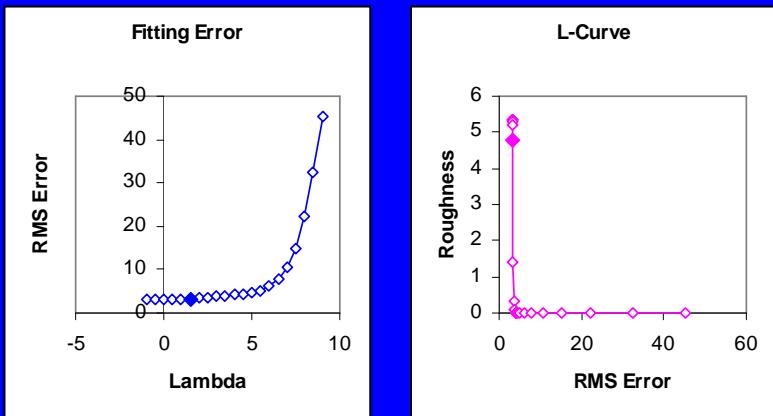
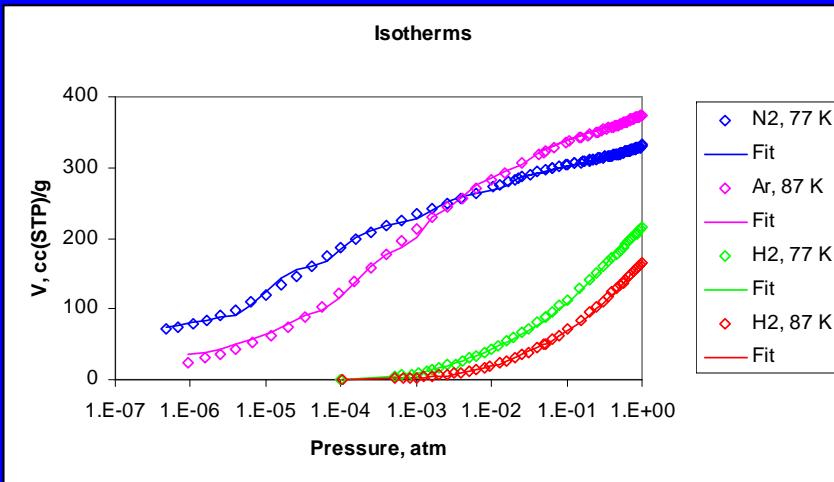
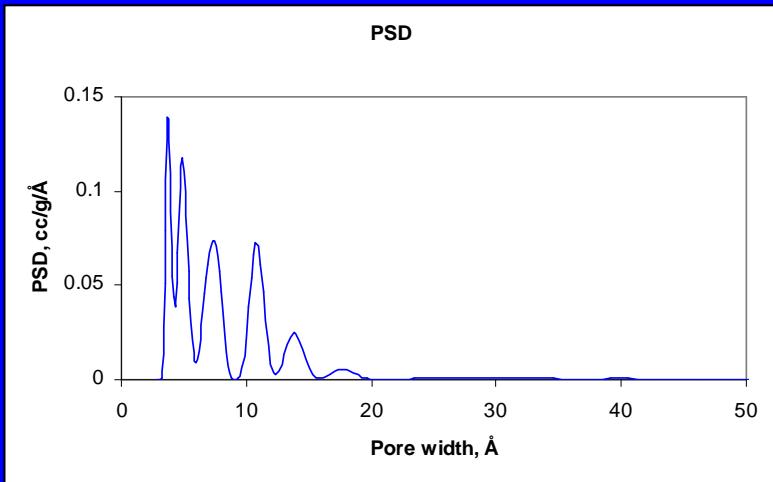
# Effect of regularization

$$\lambda = 1$$



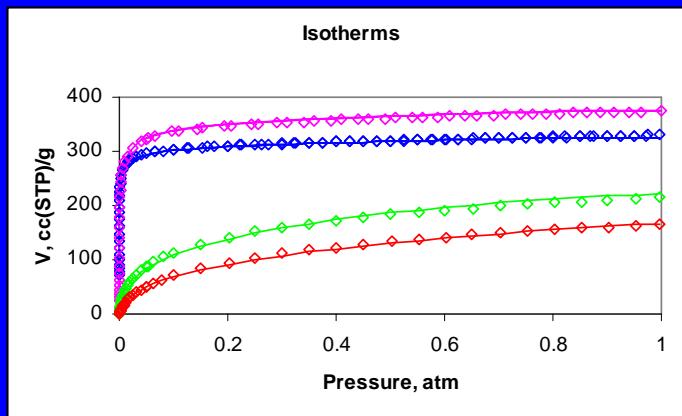
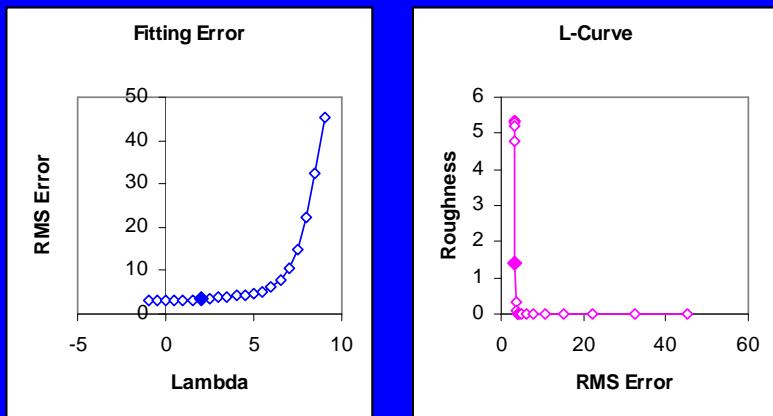
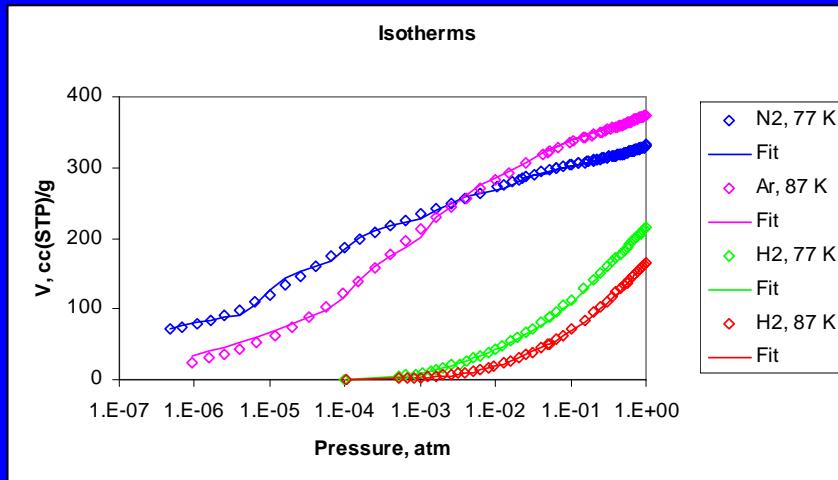
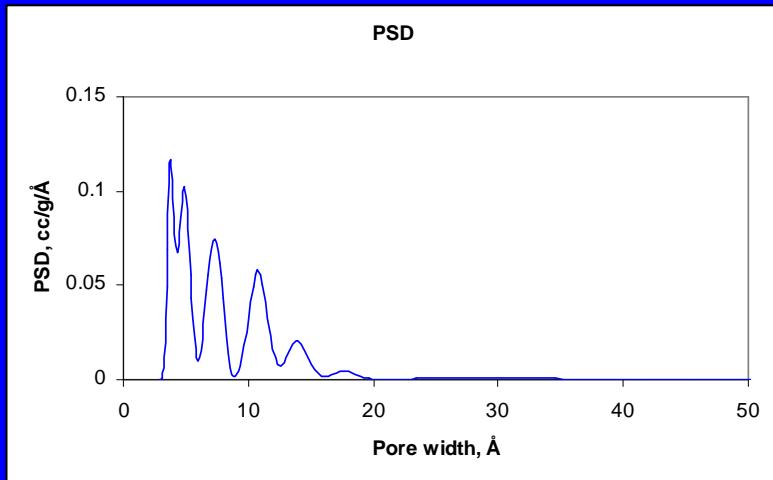
# Effect of regularization

$$\lambda = 1.5$$



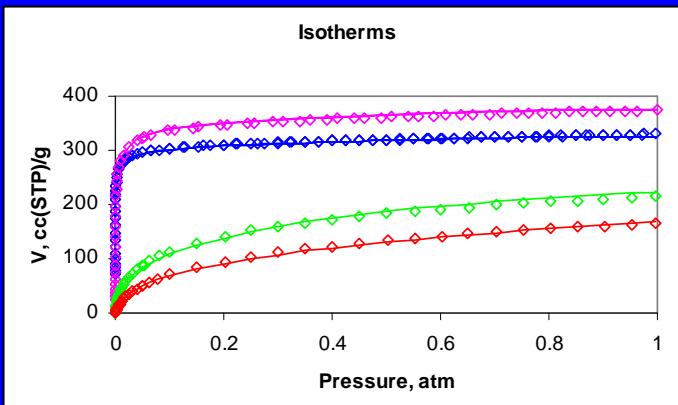
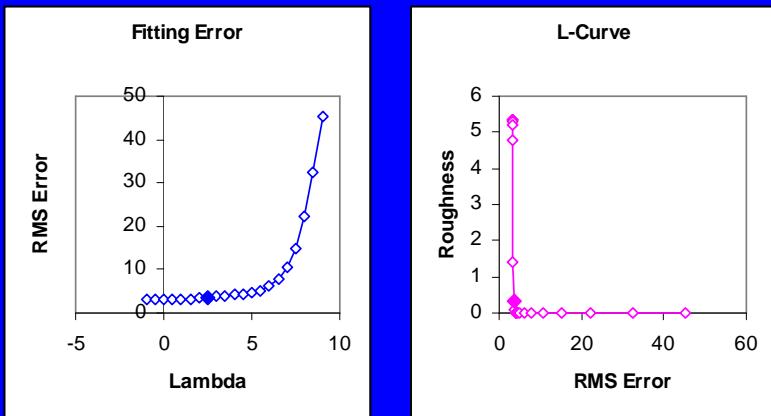
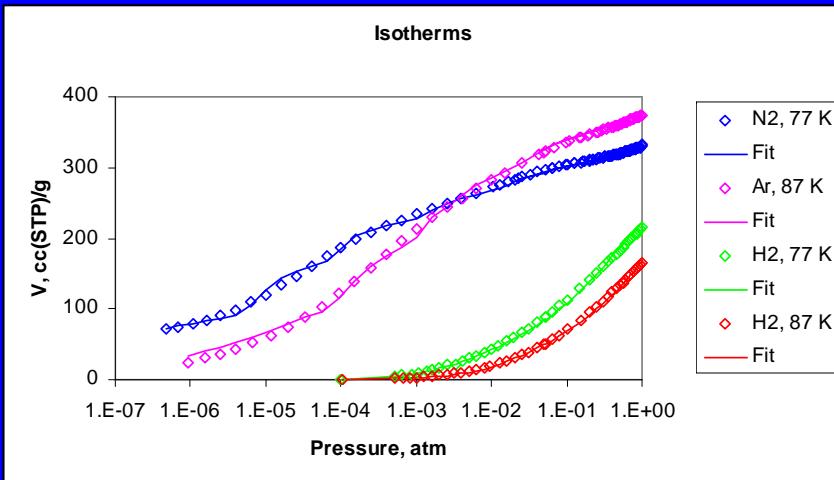
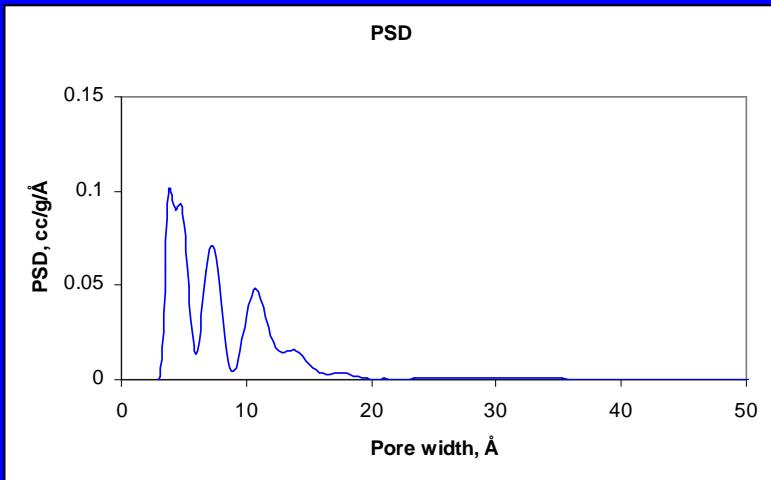
# Effect of regularization

$$\lambda = 2$$



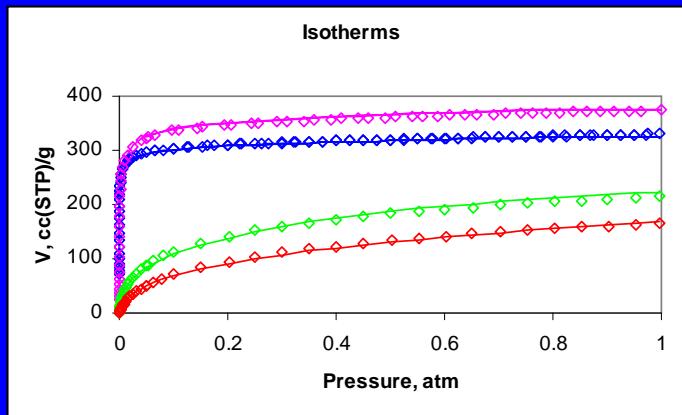
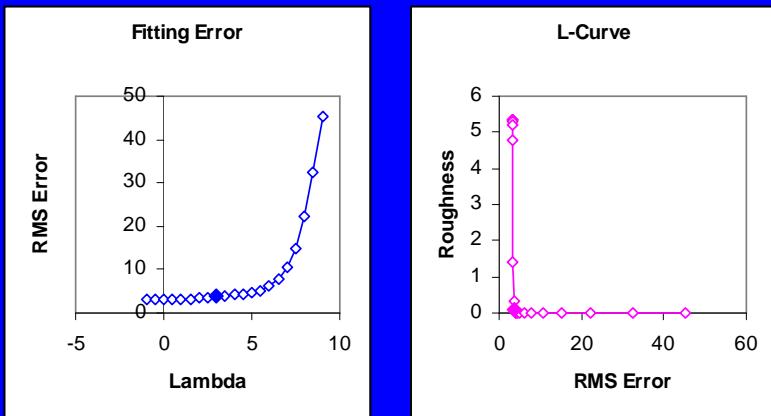
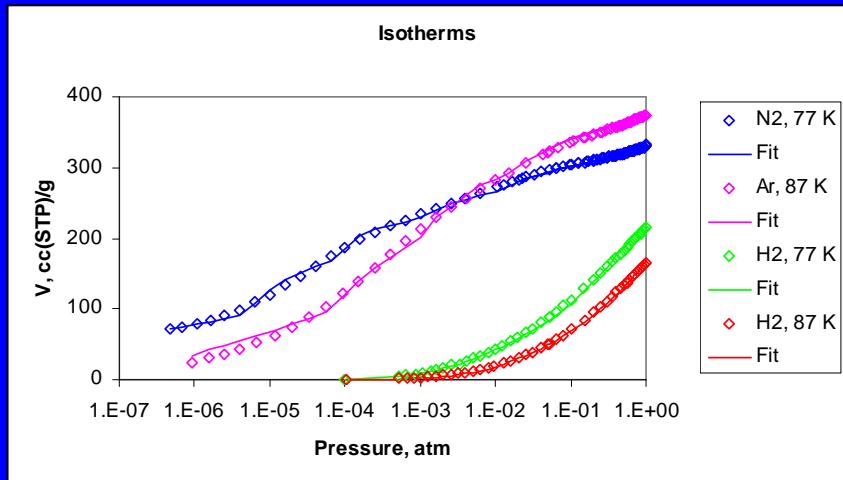
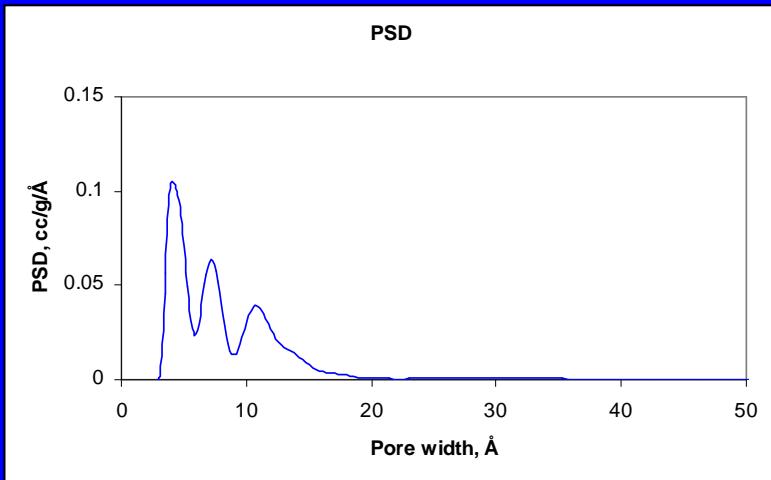
# Effect of regularization

$$\lambda = 2.5$$



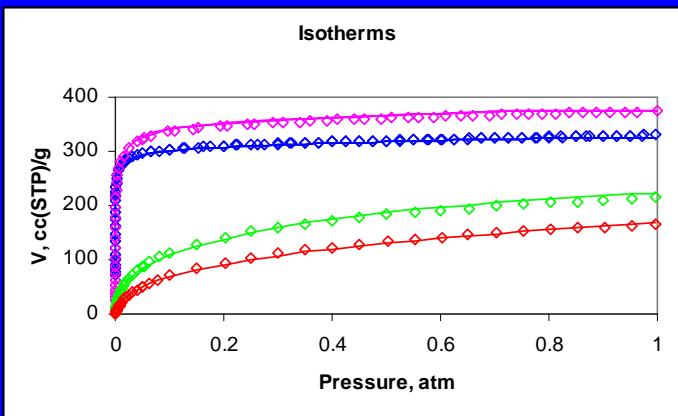
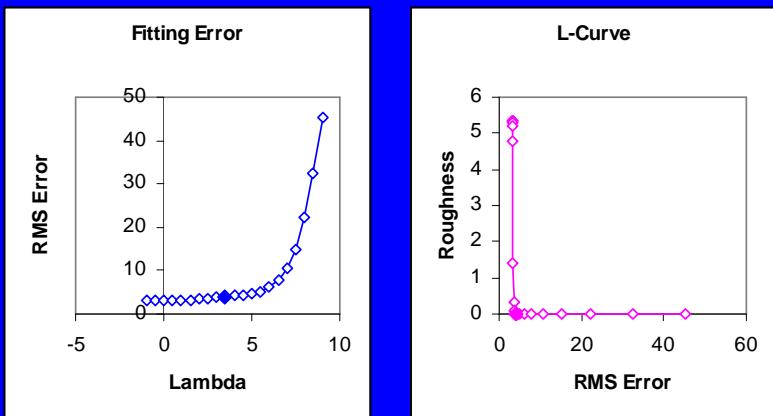
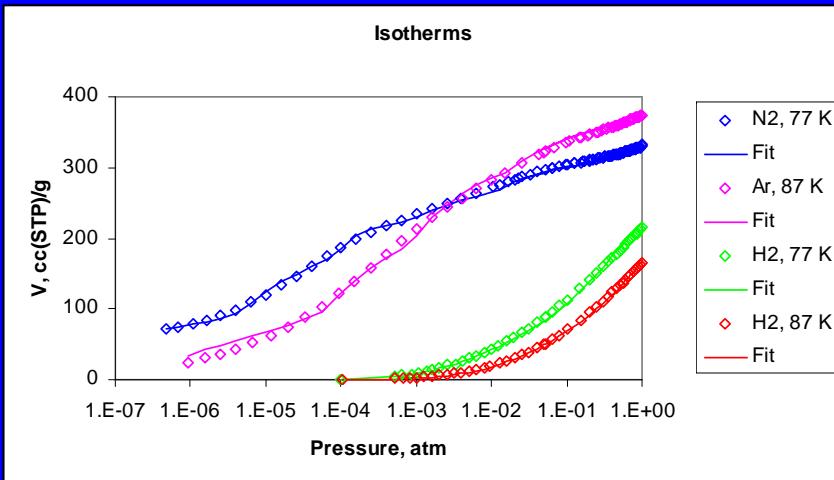
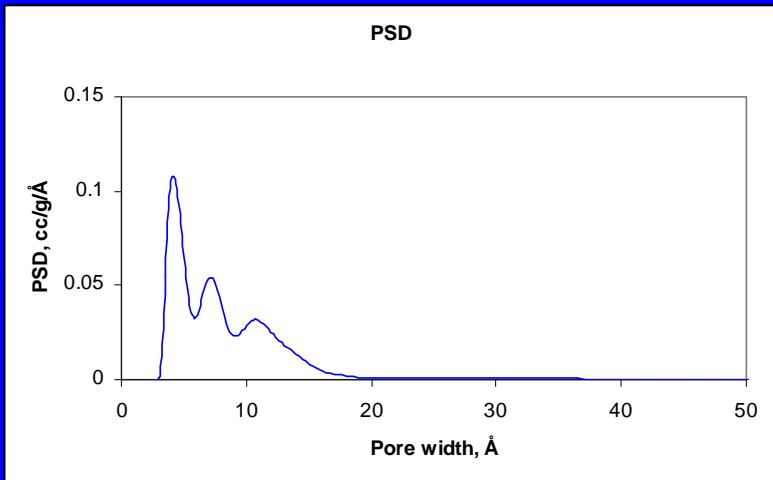
# Effect of regularization

$\lambda = 3$



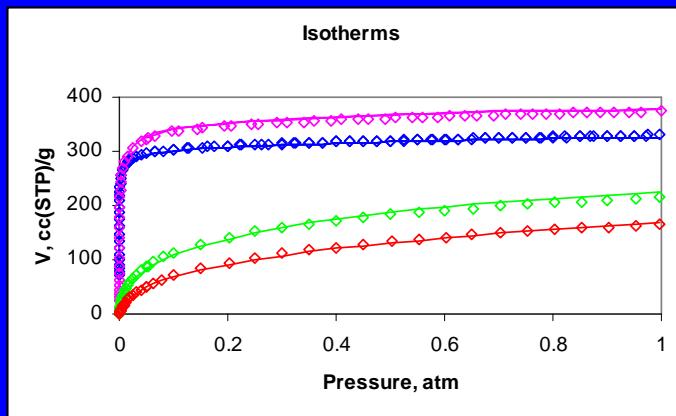
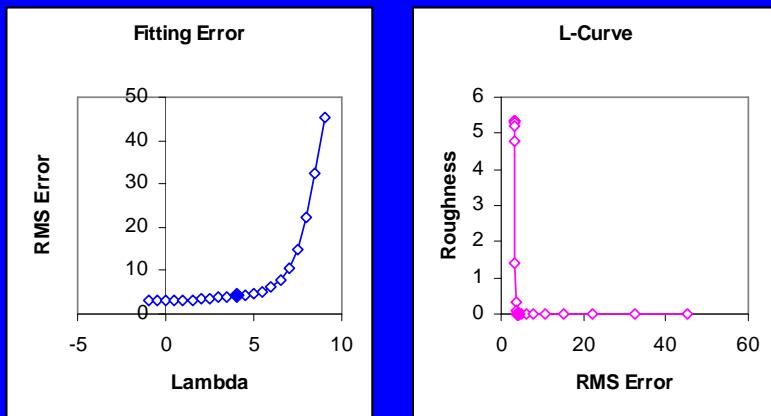
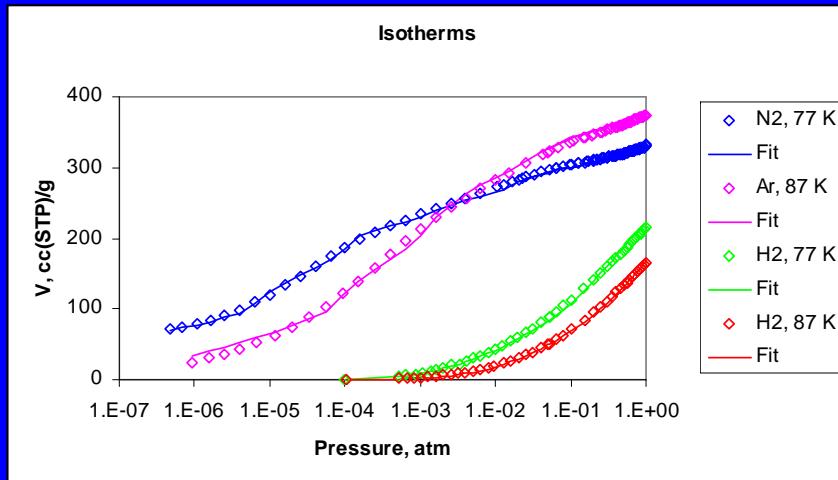
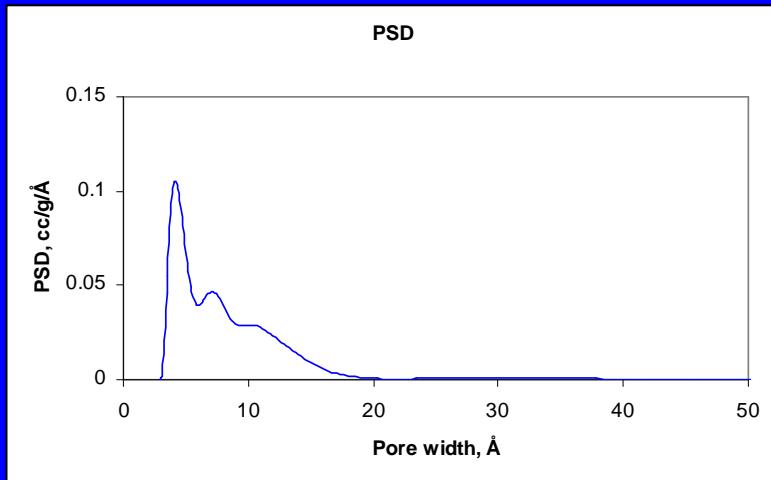
# Effect of regularization

$$\lambda = 3.5$$



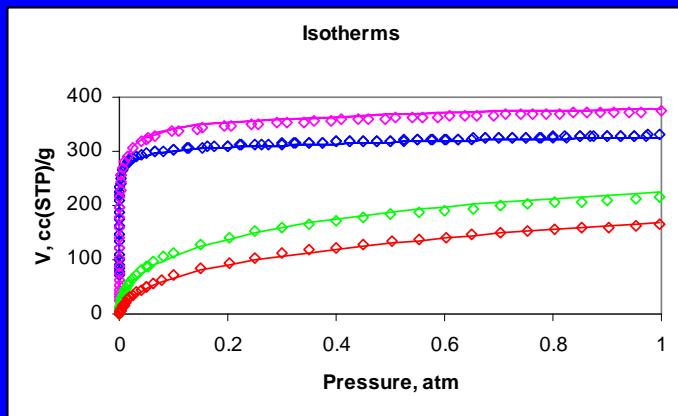
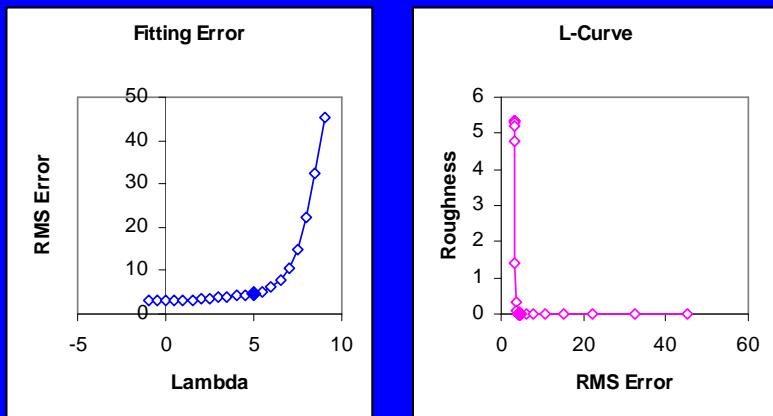
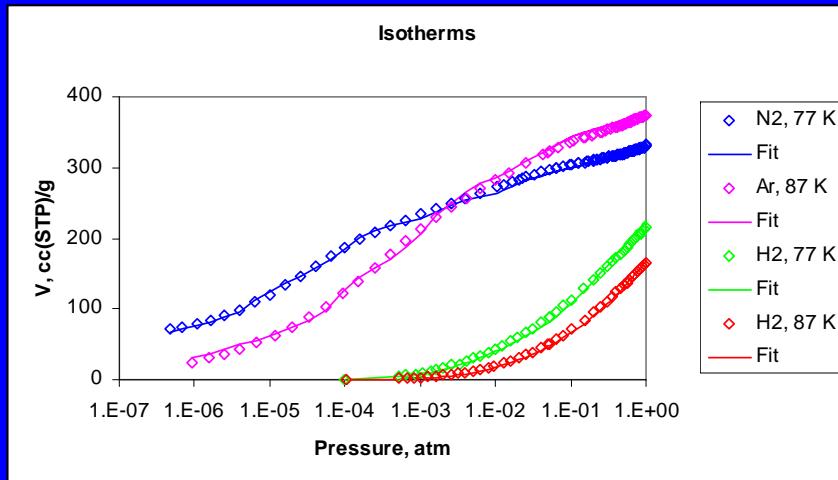
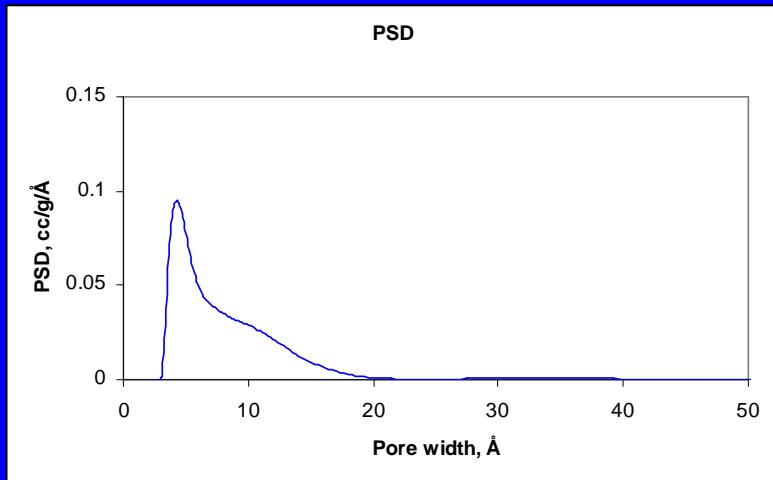
# Effect of regularization

$$\lambda = 4$$



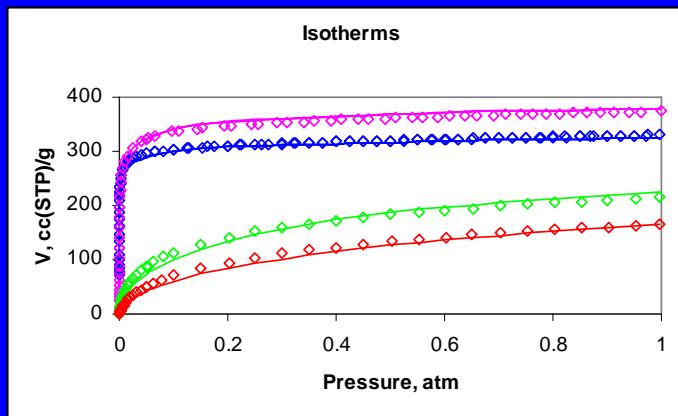
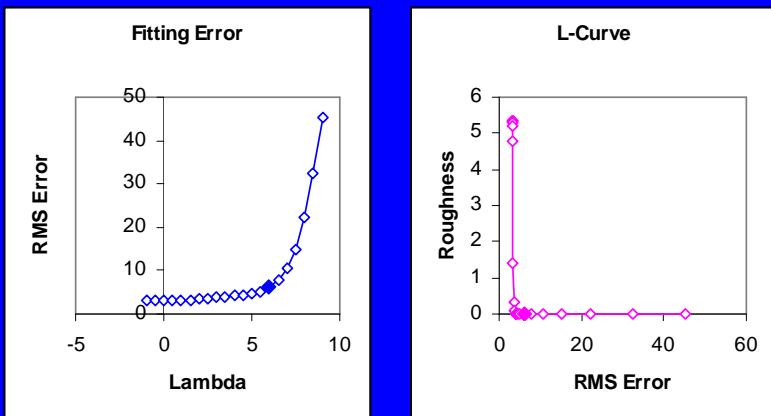
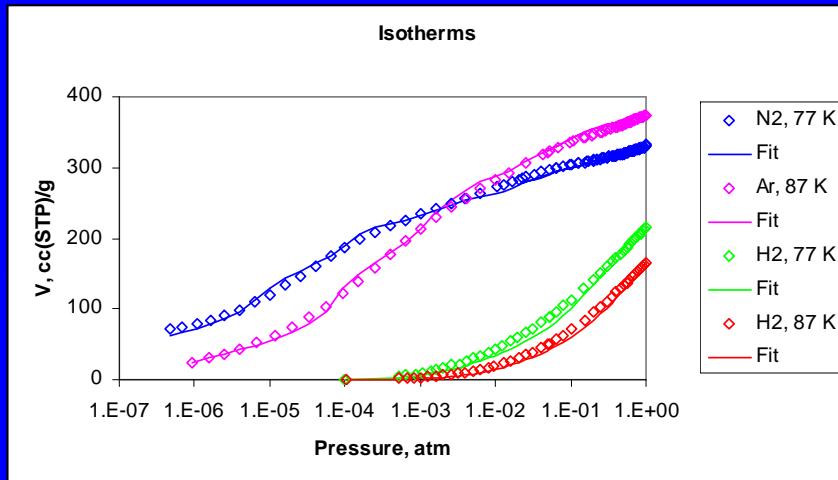
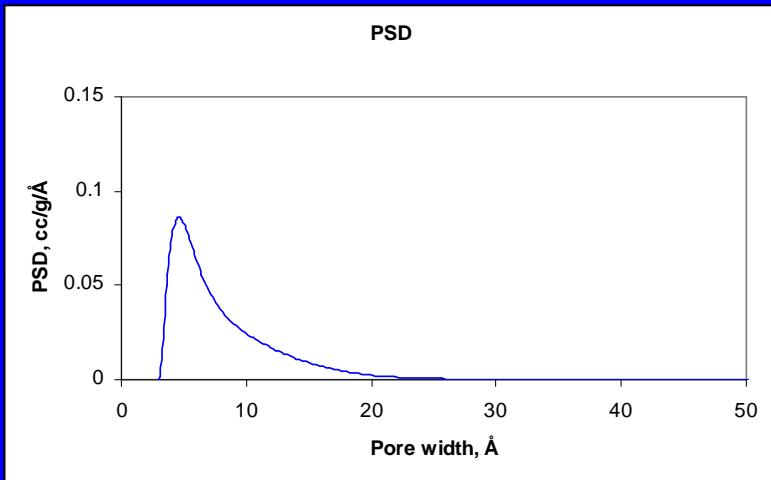
# Effect of regularization

$\lambda = 5$



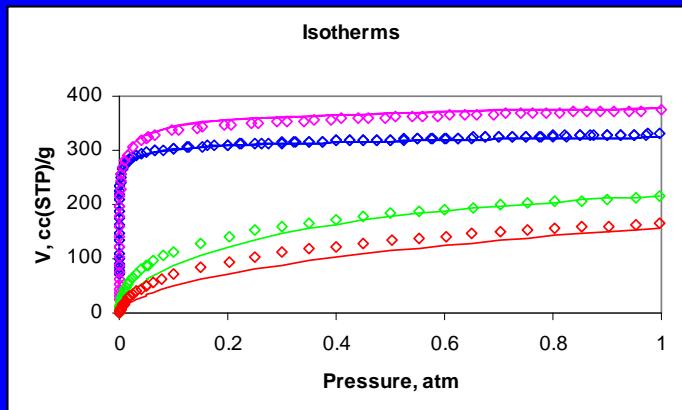
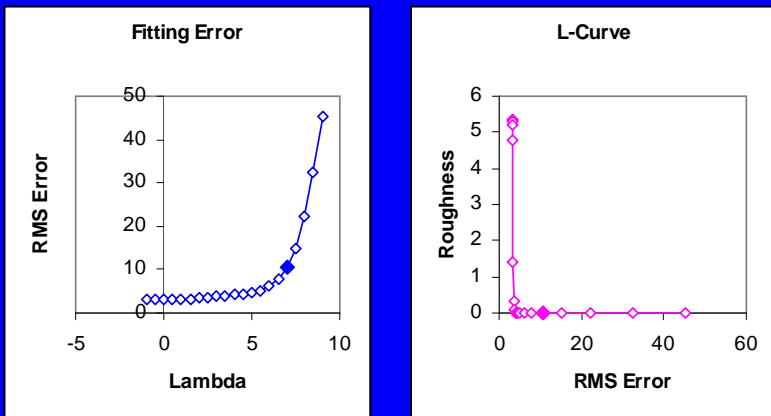
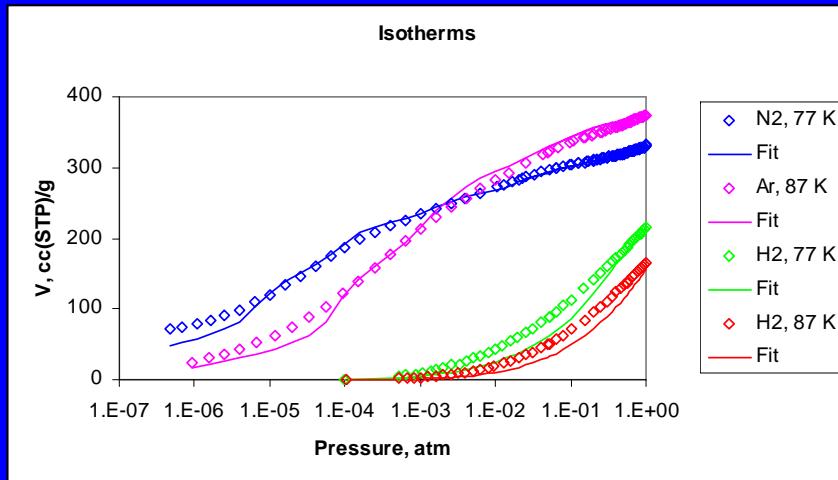
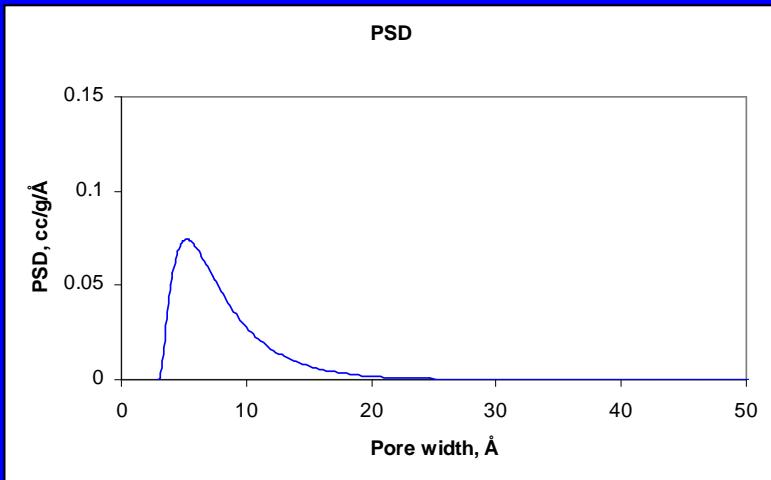
# Effect of regularization

$$\lambda = 6$$



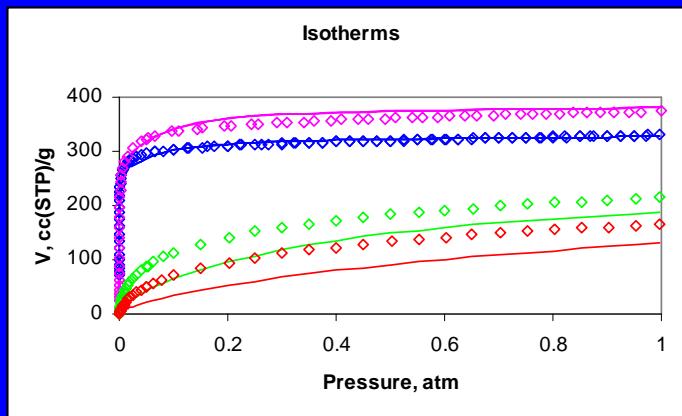
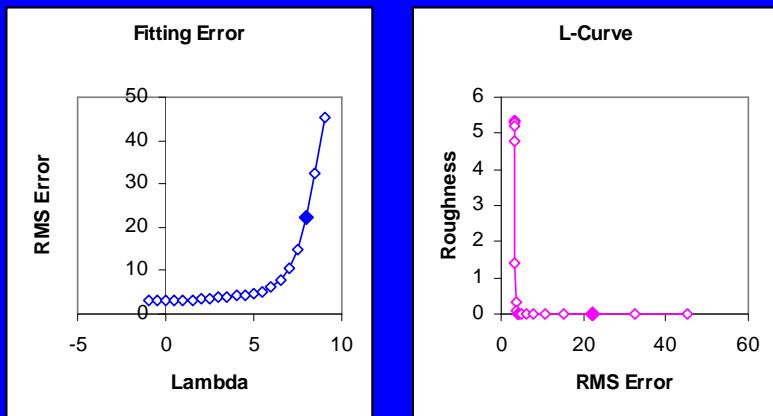
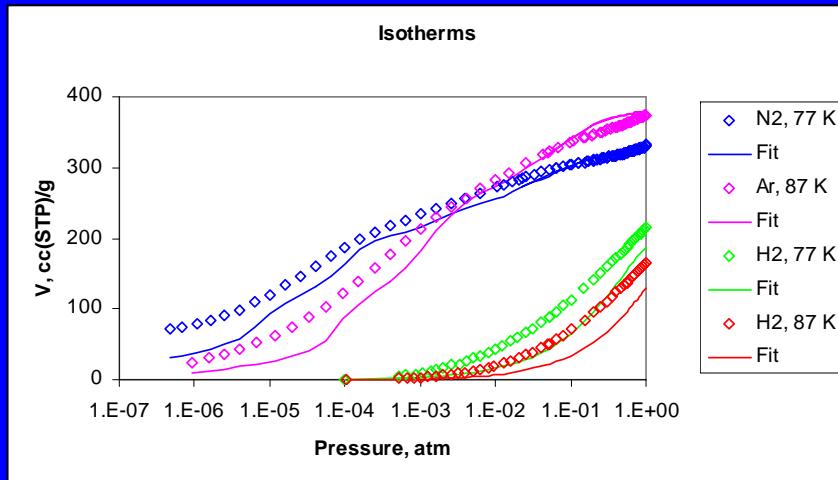
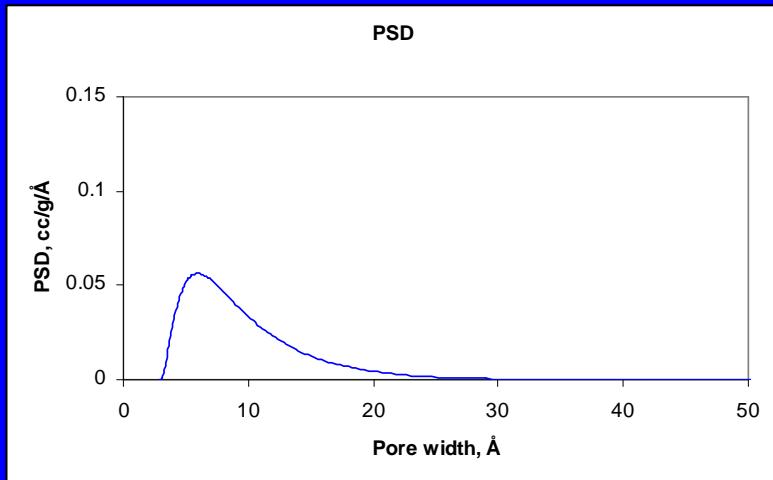
# Effect of regularization

$$\lambda = 7$$



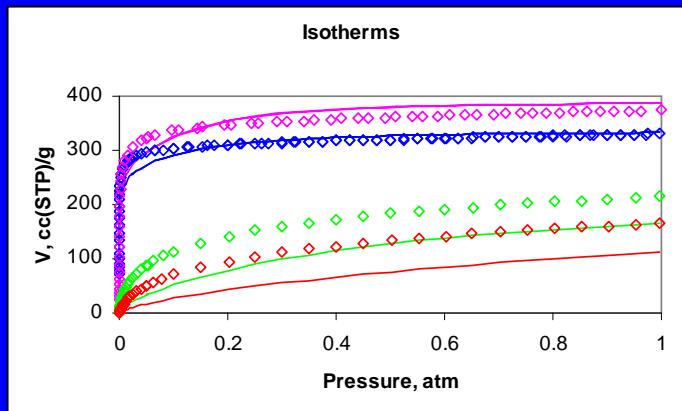
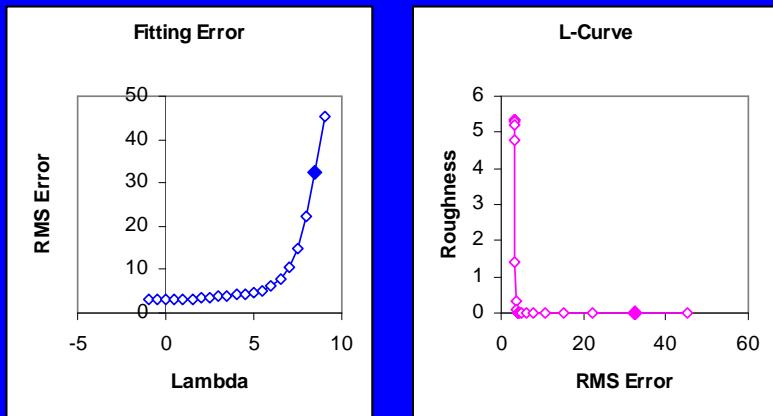
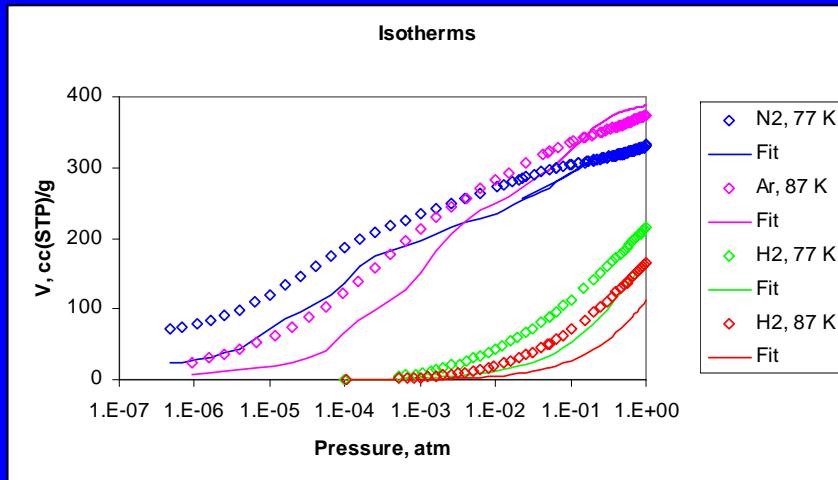
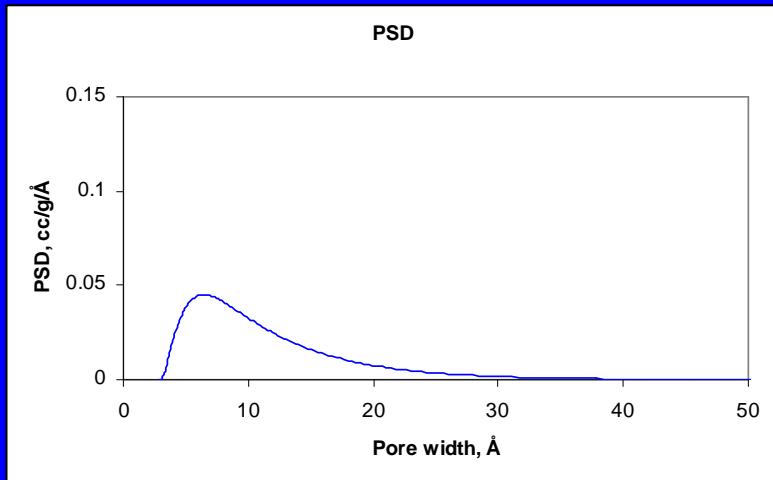
# Effect of regularization

$\lambda = 7.5$



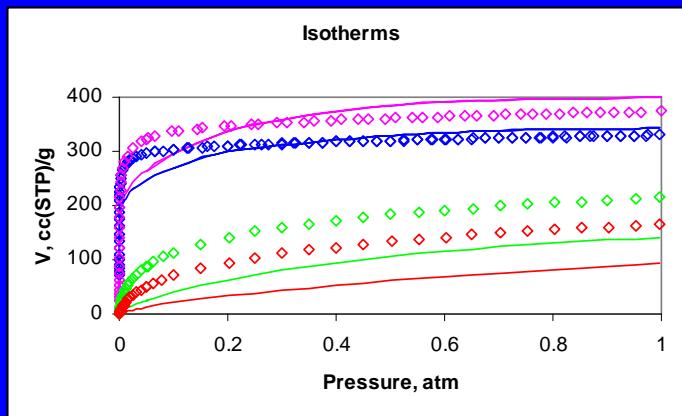
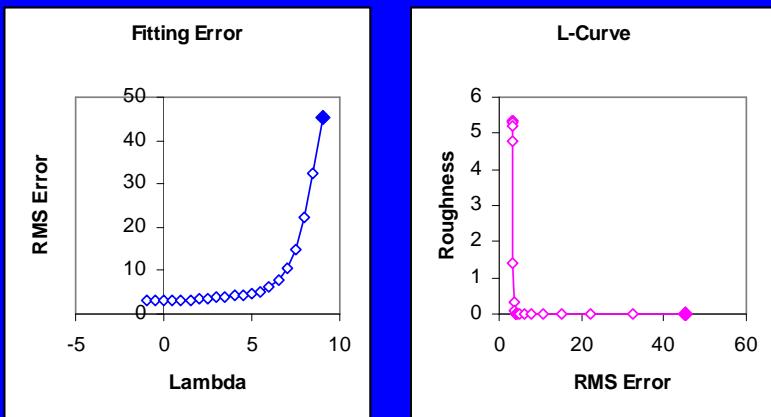
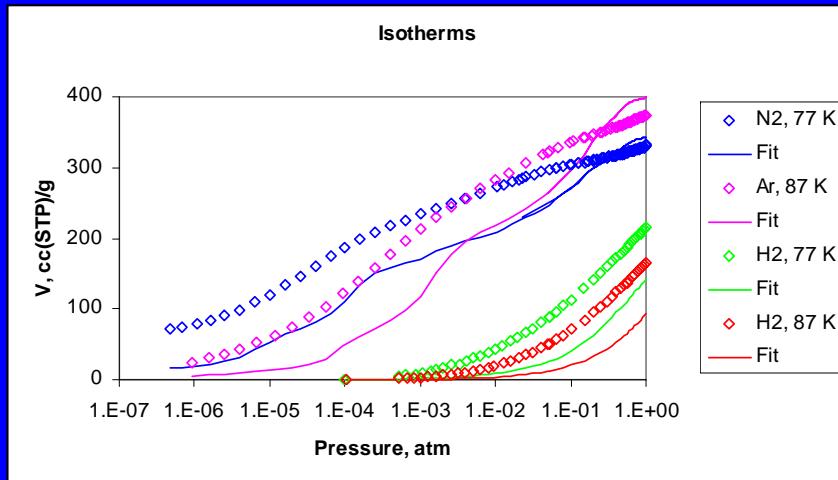
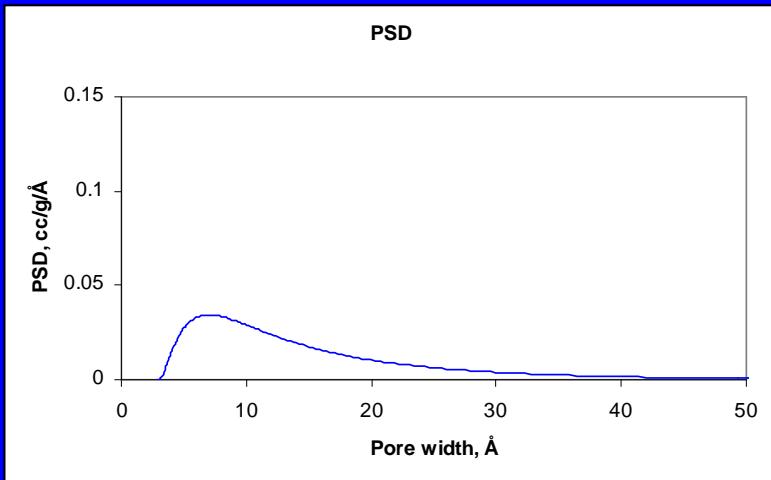
# Effect of regularization

$\lambda = 9$



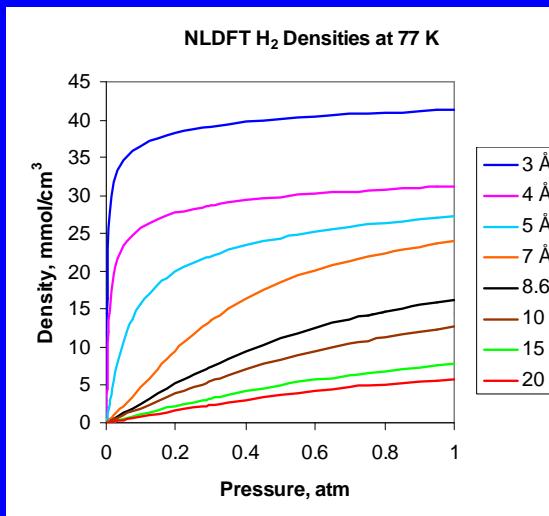
# Effect of regularization

$\lambda = 9$

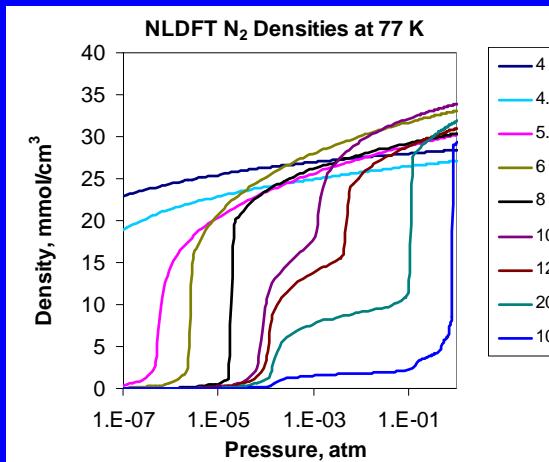


# Using Isotherms at Sub and Super Critical Temperatures

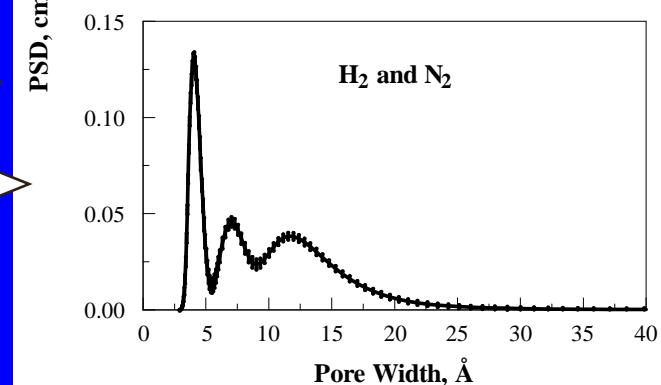
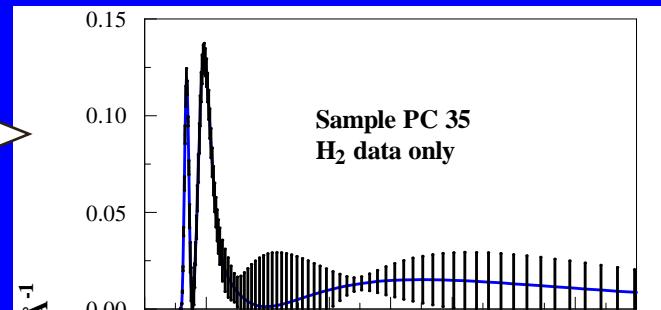
H<sub>2</sub> at 77 K  
(Super Critical)



N<sub>2</sub> at 77 K  
(Sub Critical)



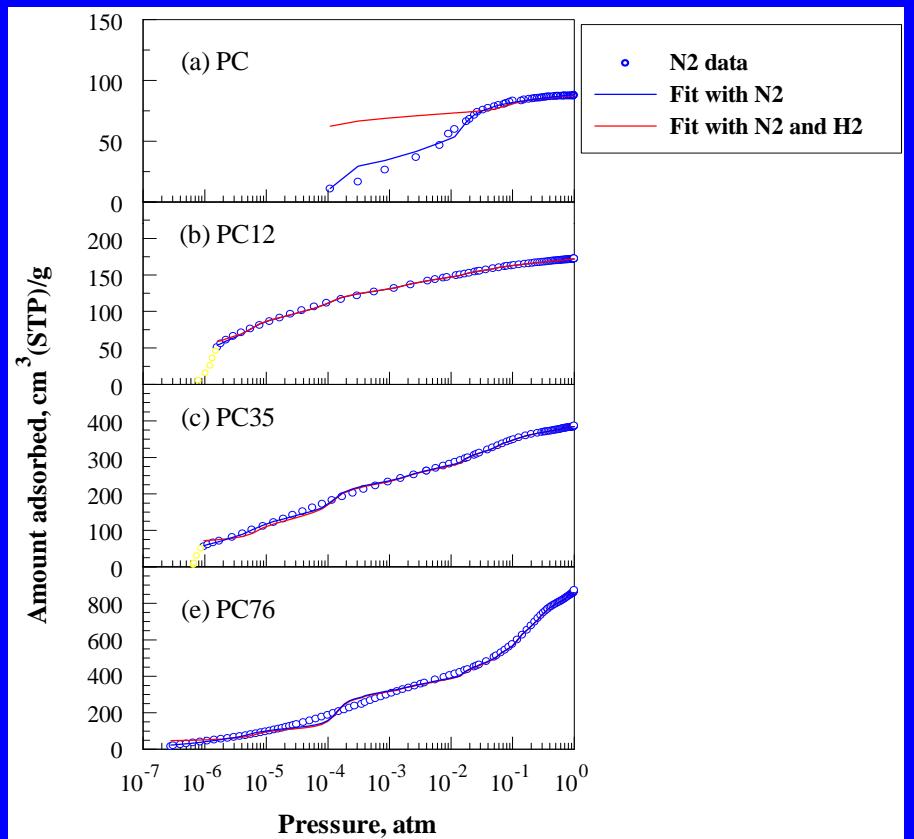
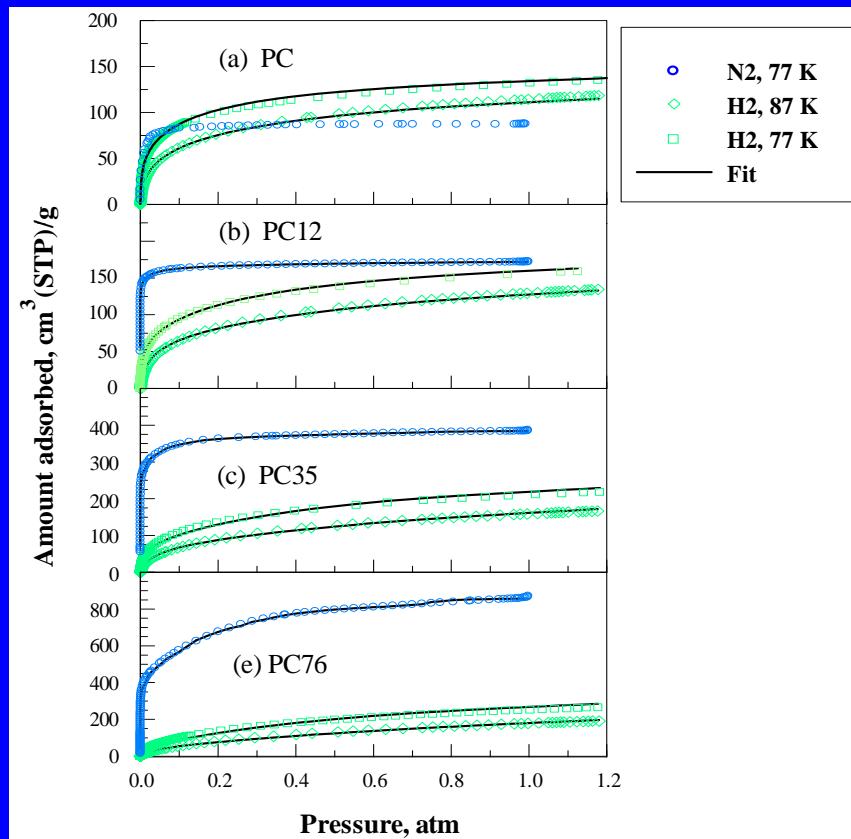
Multi Adsorbate Fit  
reduces uncertainty of calculated  
PSD



Error bars from the covariance matrix

# Analysis of adsorption isotherms for series of PC carbons

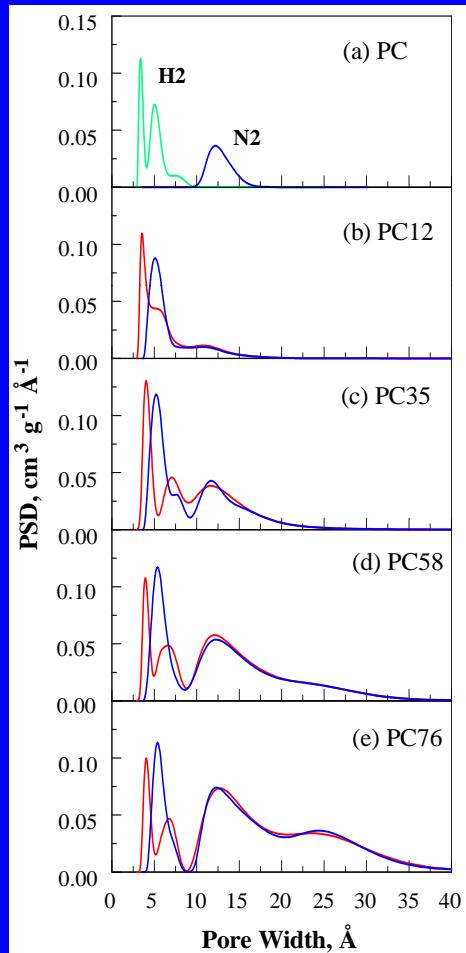
Multi versus single adsorbate fit



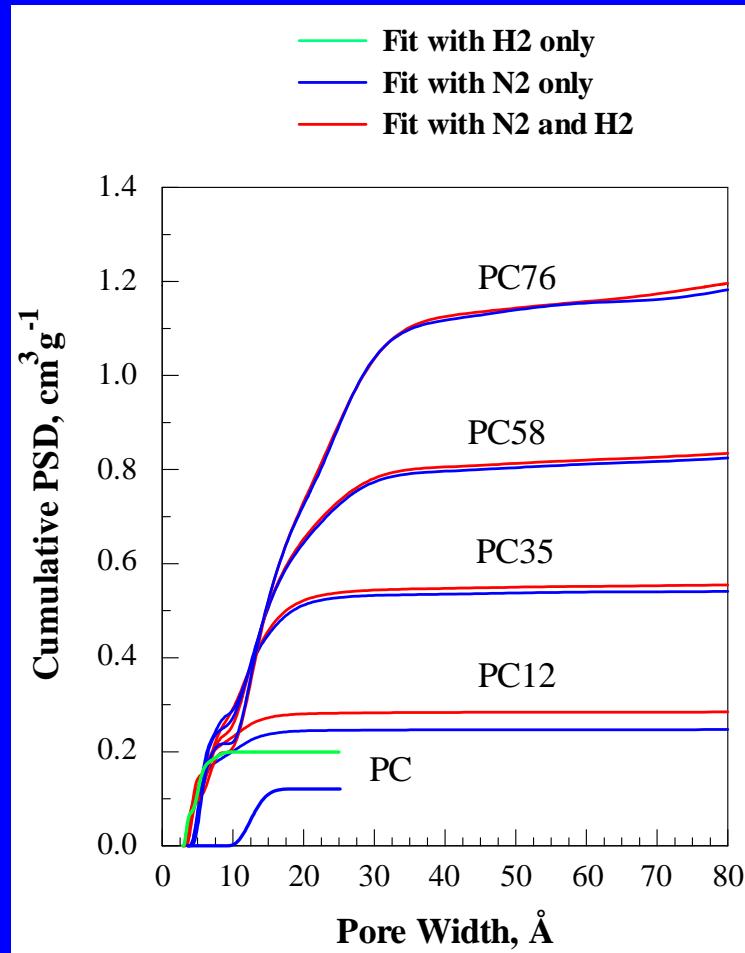
J. Jagiello, C. O. Ania, J. B. Parra, L. Jagiello, J. J. Pis, Carbon 45, 1066-1077 (2007)

# Calculated PSDs for PC samples

Differential

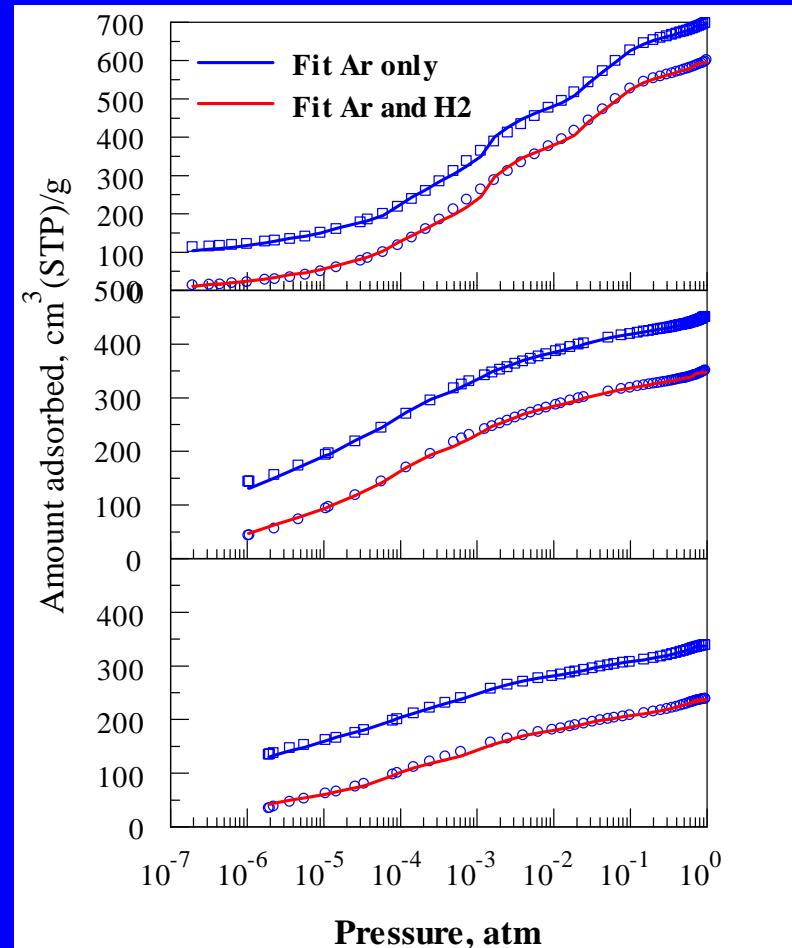
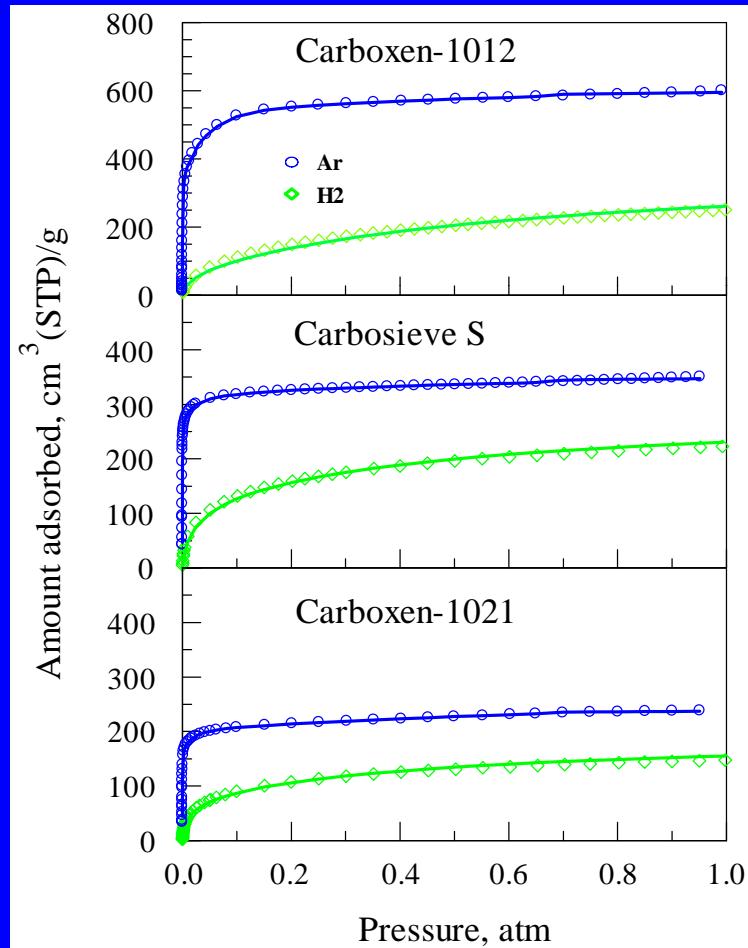


Cumulative



J. Jagiello, C. O. Ania, J. B. Parra, L. Jagiello, J. J. Pis, Carbon 45, 1066-1077 (2007)

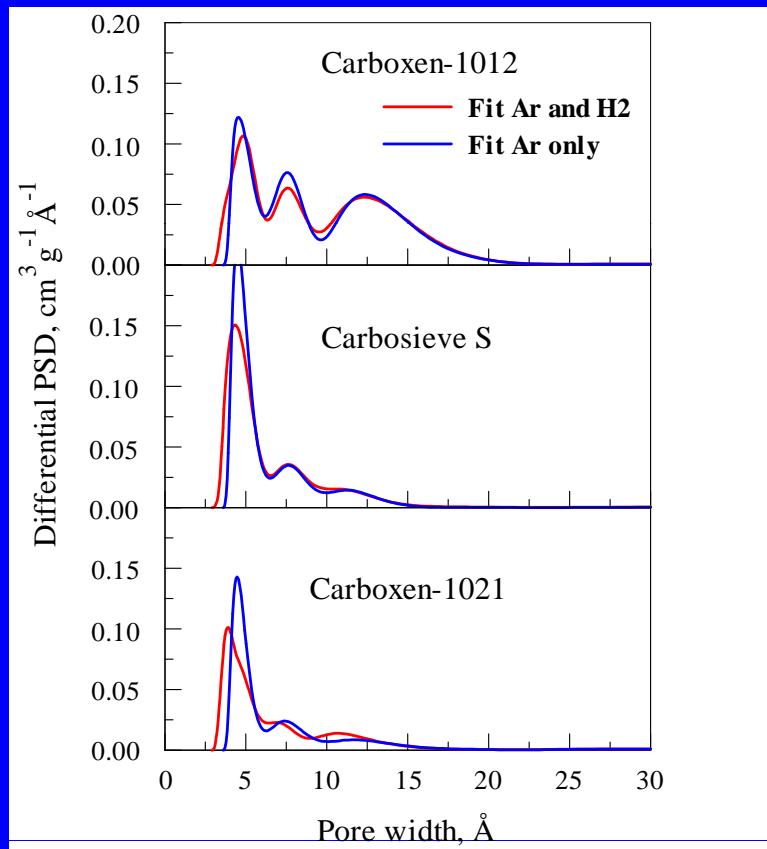
# Fitting Ar and H<sub>2</sub> isotherms measured on CMS samples



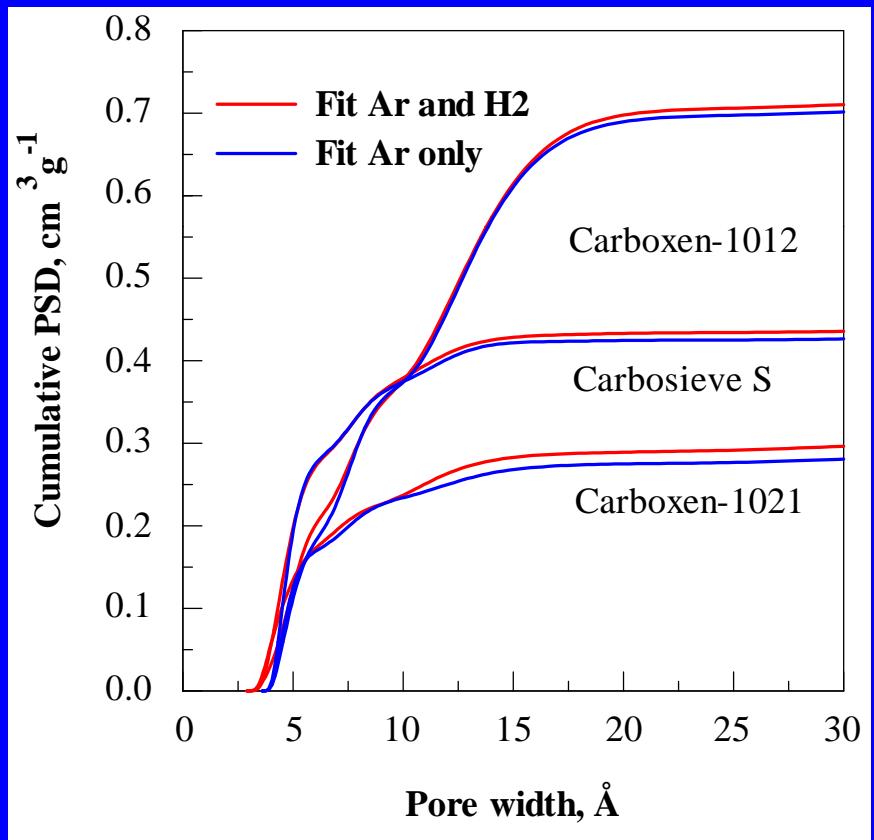
J. Jagiello, W. Betz, Microporous and Mesoporous Materials **108**, 117–122 (2008)

# Calculated PSDs for CMS samples

Differential



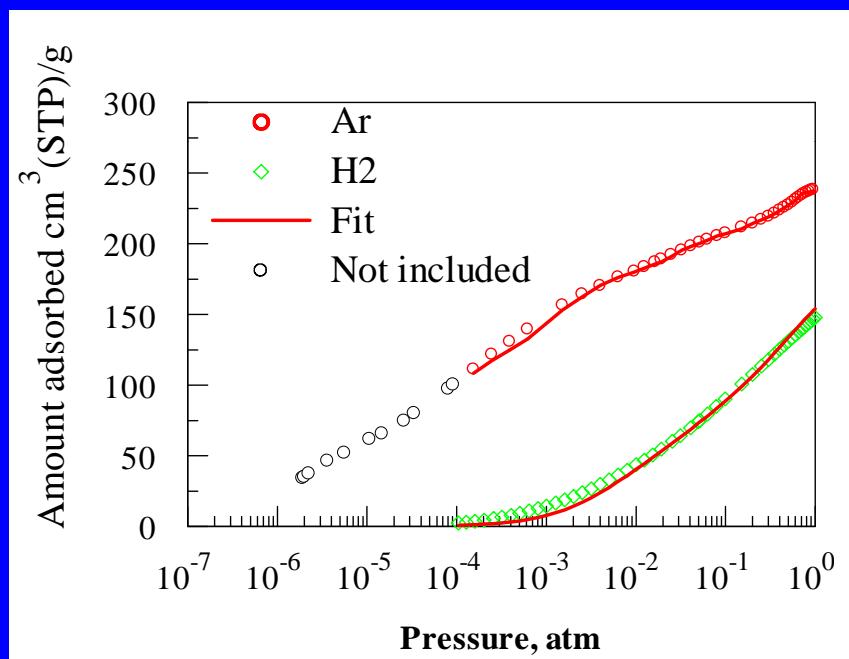
Cumulative



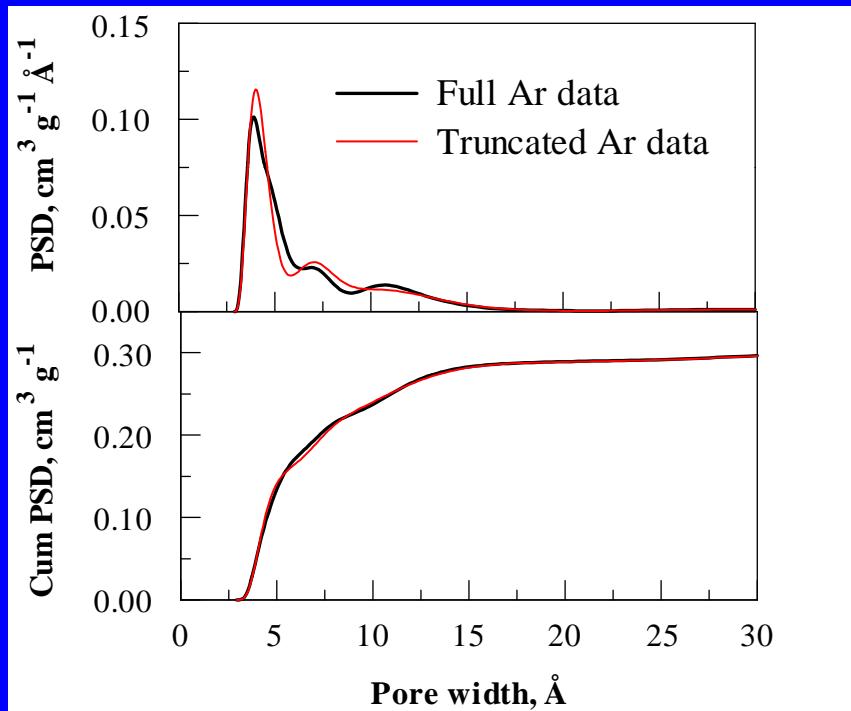
J. Jagiello, W. Betz, Microporous and Mesoporous Materials **108**, 117–122 (2008)

# Effect of using truncated Ar data (Carboxen-1021)

Isotherm data used



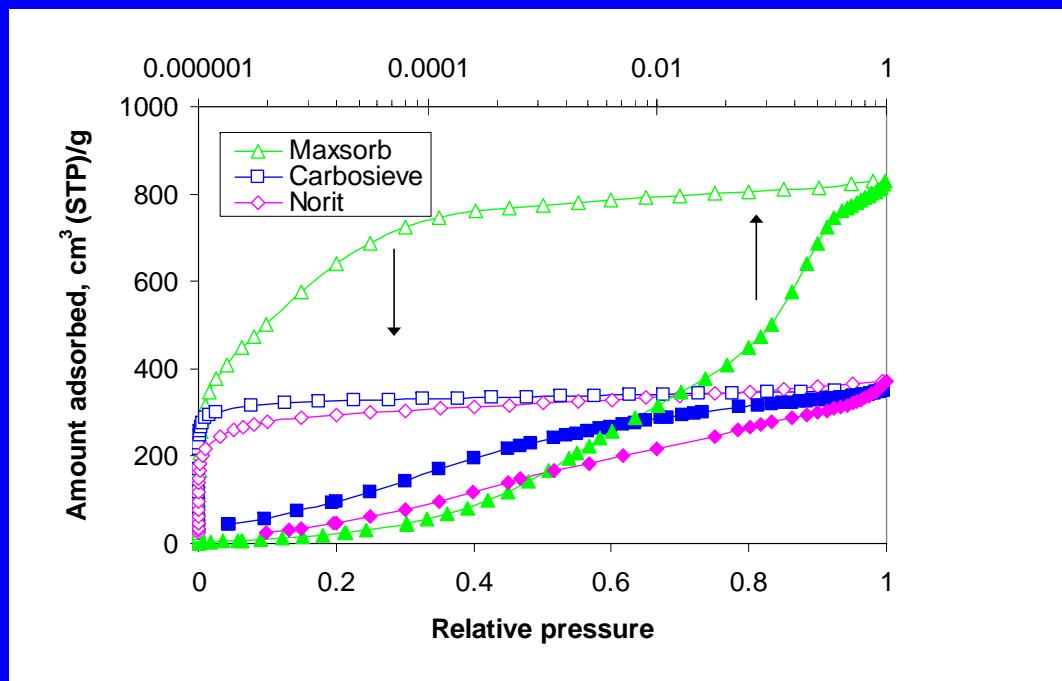
Calculated PSD



J. Jagiello, W. Betz, Microporous and Mesoporous Materials 108, 117–122 (2008)

# Prediction of High-Pressure H<sub>2</sub> Adsorption

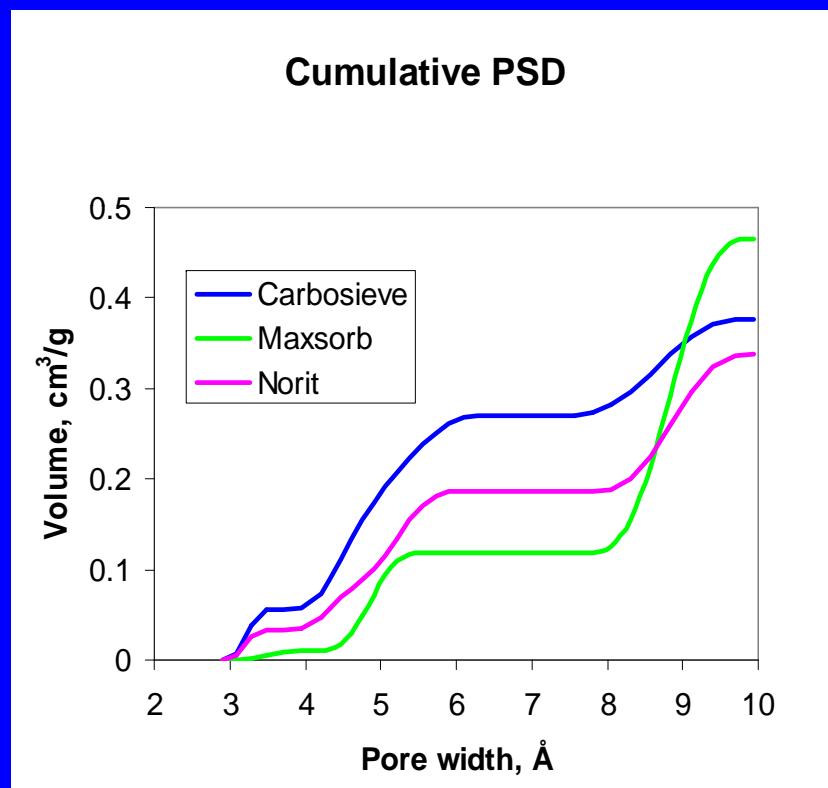
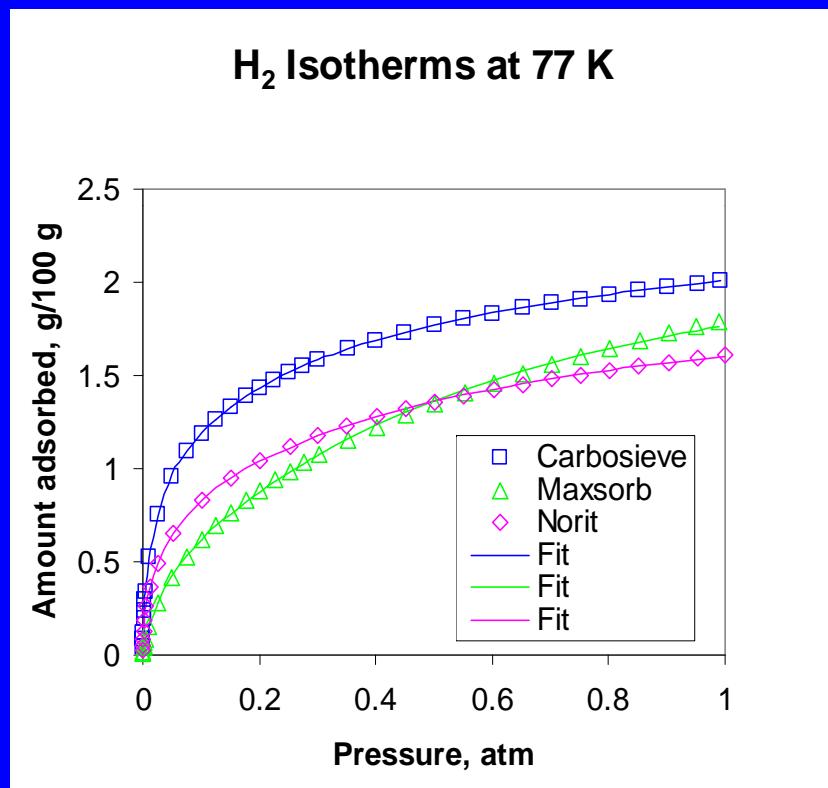
Standard Adsorption Properties Derived from Ar Isotherms (87 K)



Sample	S(BET) m <sup>2</sup> /g	V <sub>m</sub> (DR) cm <sup>3</sup> /g
Maxsorb	2100	0.69
CarboSieve	1120	0.42
Norit	970	0.37

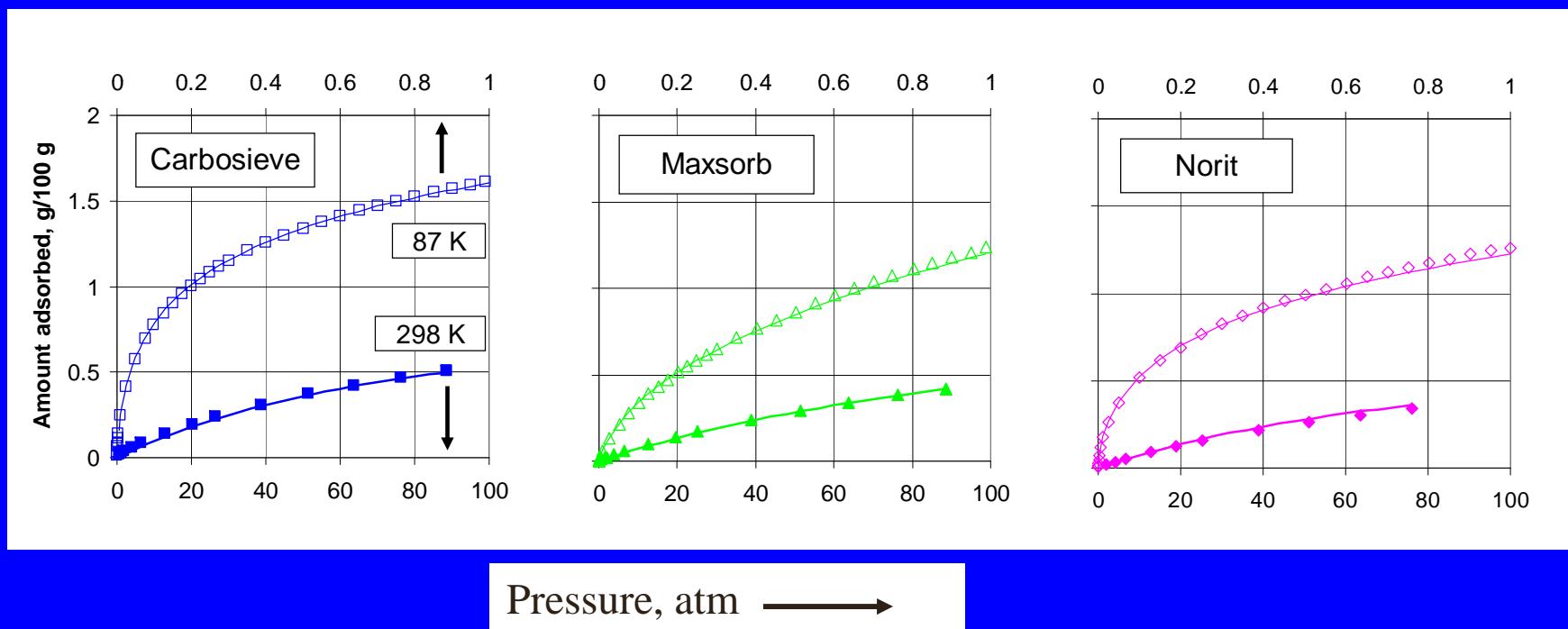
J. Jagiello, A. Anson, M.T. Martinez, J. Phys. Chem., 110 (2006) 4531

# Micro pore Analysis Using H<sub>2</sub> Adsorption



J. Jagiello, A. Anson, M.T. Martinez, J. Phys. Chem., 110 (2006) 4531

# Prediction of H<sub>2</sub> Adsorption at 87 and 298 K from Adsorption Isotherms at 77 K Based on DFT Model



J. Jagiello, A. Anson, M.T. Martinez, J. Phys. Chem., 110 (2006) 4531

# Effects of pore size and chemistry in analysis of zeolite pore structure

Cylindrical pore model is assumed for zeolite pores.

Model NLDFT isotherms (kernels) are calculated using Tarazona approach.

Fluid-pore interaction potential has the following form:

$$U_{\text{pore}} = E_{\text{wall}}(\rho, \varepsilon_{sf}) U_{\text{cylinder}}(w, r)$$

where:

$\rho$  - the solid density

$\varepsilon_{sf}$  - the adsorbate-solid atom interaction parameter

w - the effective pore width

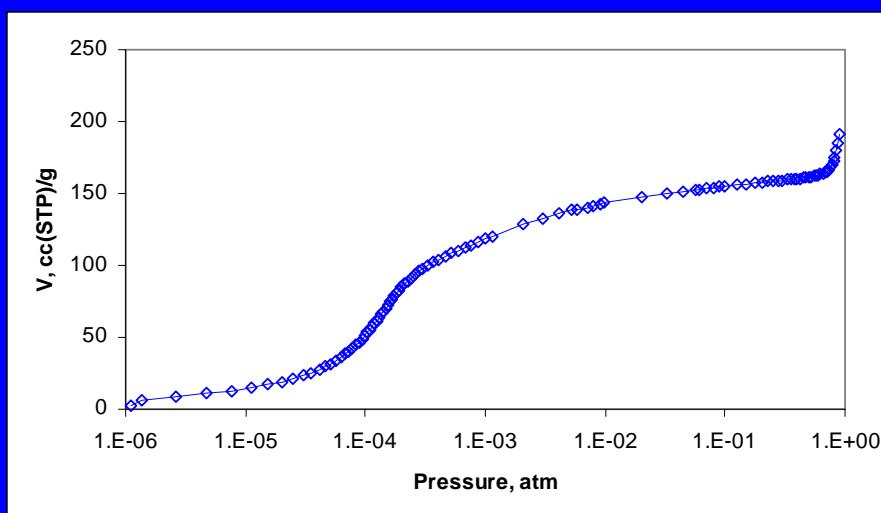
r - the distance of a molecule from the pore wall

$E_{\text{wall}}$  – the wall potential interaction parameter

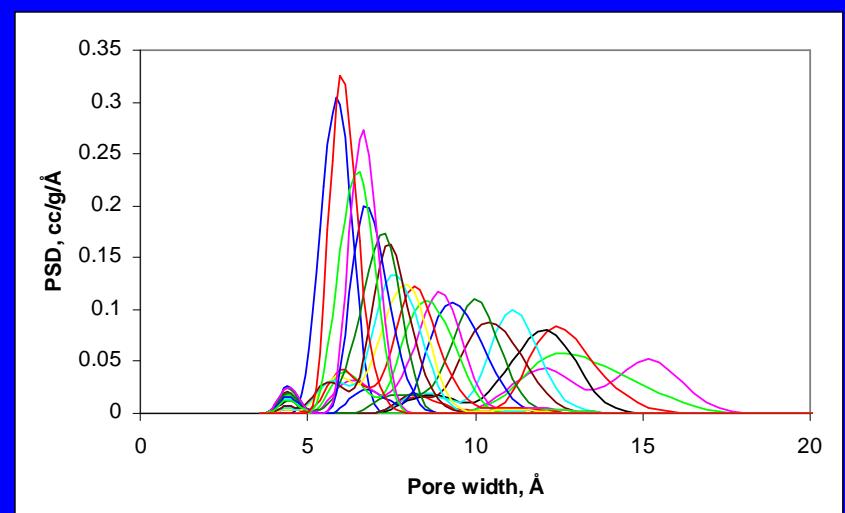
$U_{\text{cylinder}}$  - the fluid-cylindrical wall interaction potential

# Effects of pore size and chemistry on gas adsorption in zeolites

N<sub>2</sub> Adsorption Isotherm  
Measured for Zeolite Y Sample

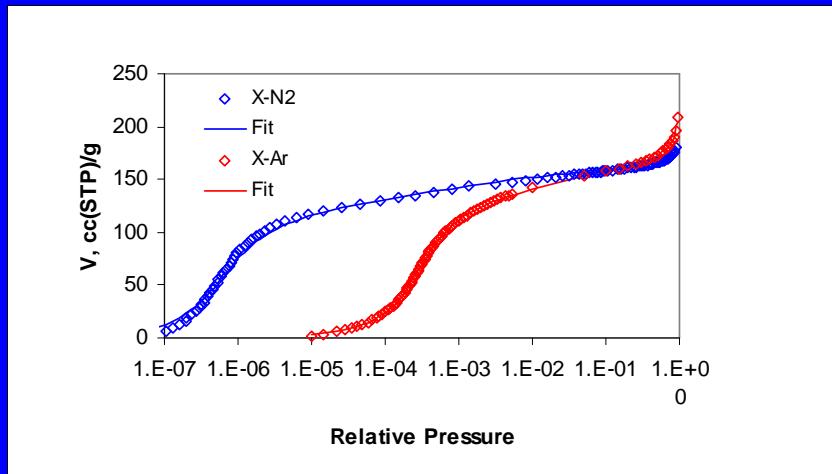


PSDs calculated for Y-N<sub>2</sub> data using different  $E_{\text{wall}}$  parameters

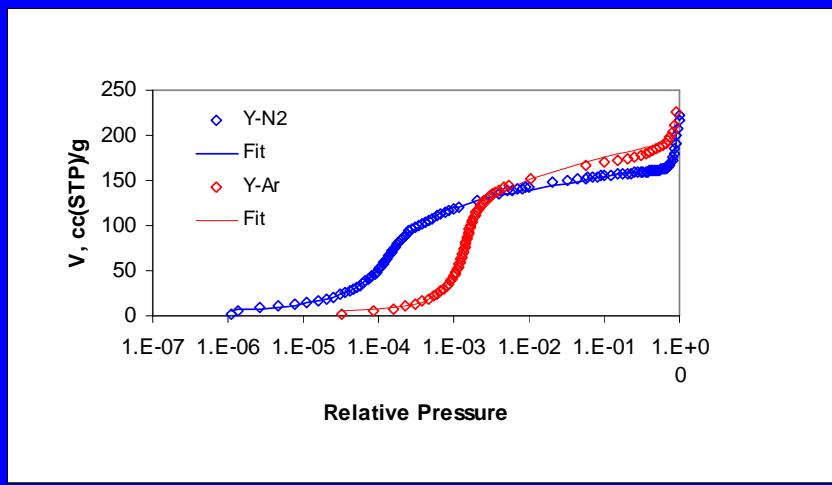


# Analysis of N<sub>2</sub> and Ar Adsorption Isotherms for Zeolite X and Y Samples

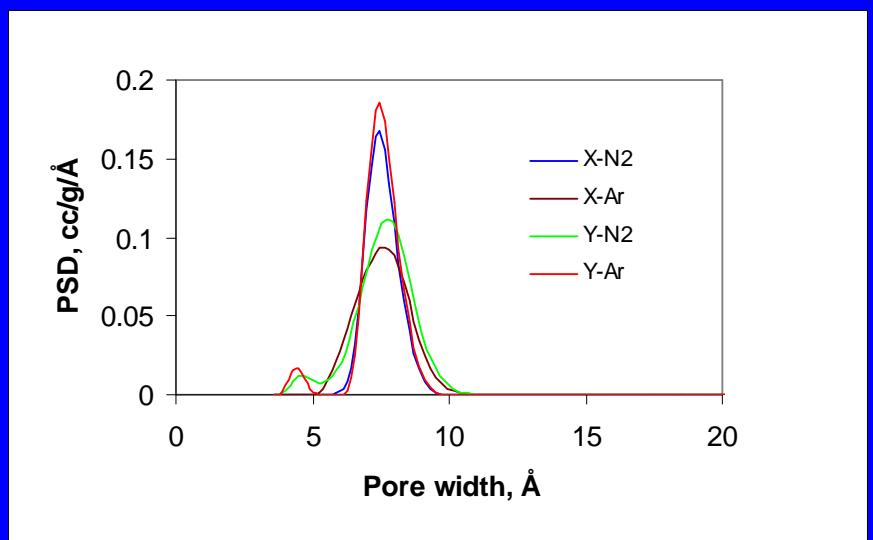
## Adsorption Isotherms for Zeolite X



## Adsorption Isotherms for Zeolite Y

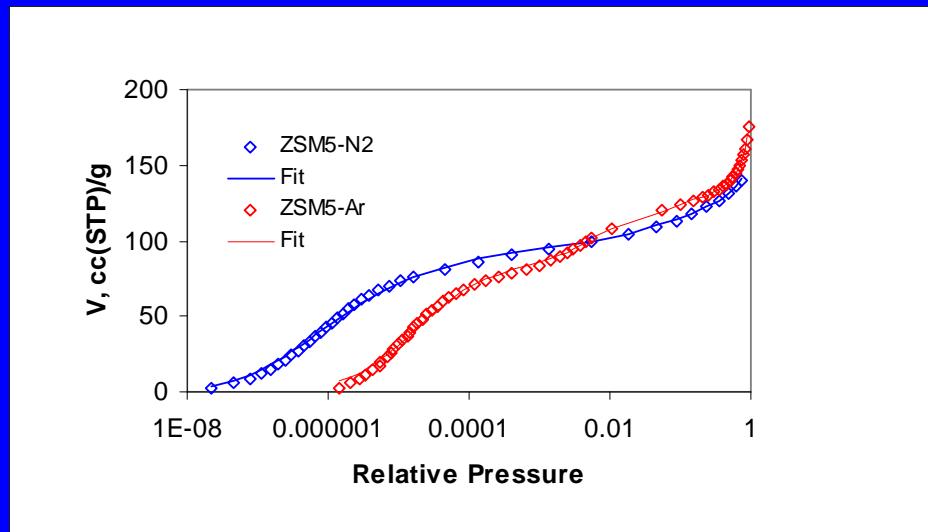


PSDs Calculated using  
Optimal  $E_{\text{wall}}$  parameters

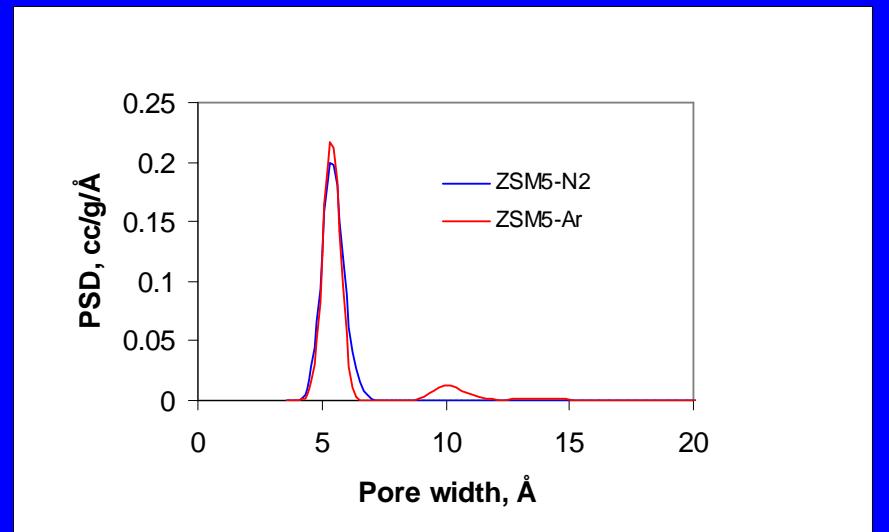


# Analysis of N<sub>2</sub> and Ar Adsorption Isotherms for ZSM5 Sample (NH<sub>4</sub> form)

N<sub>2</sub> and Ar Adsorption Isotherms

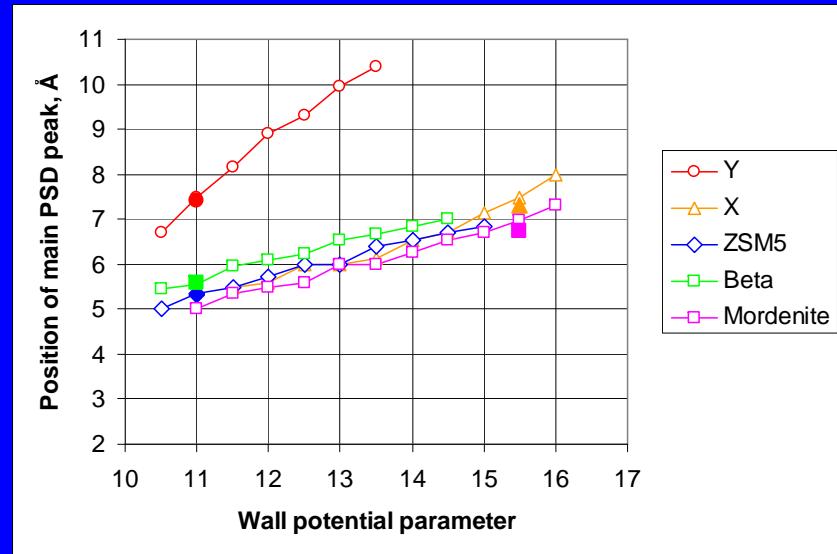


PSDs Calculated using  
Optimal  $E_{\text{wall}}$  parameters

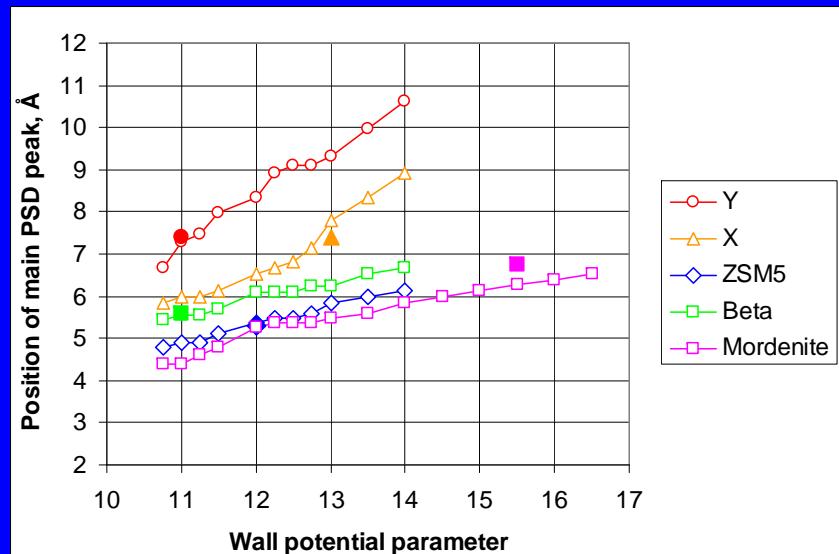


# PSD Peak Position as a Function of Wall Potential Parameter, $E_{\text{wall}}$

$N_2$



Ar



# Conclusions

- Carbon PSDs obtained from the simultaneous analysis of multiple adsorption isotherms are robust and consistent with more than one adsorbate.
- This approach allows detecting experimental points that are not fully equilibrated due to very slow diffusion to narrow micropores.
- The range of pore size analysis is extended to smaller pore sizes compared to the standard nitrogen or argon adsorption analysis.
- Data of the two isotherms provide complementary information about the carbon porosity in the range of micro and mesopores.
- Proposed approach can be considered a useful tool for a comprehensive characterization of activated carbons, and for obtaining detailed and reliable carbon PSDs.
- Effective pore wall potential assumed for zeolites allows separating geometrical and chemical effects in the analysis of zeolite pore structure.

**PSDs calculated for Y-N2 data using different Ewall parameters.**

**N2 and Ar Adsorption Isotherms for Zeolite X Sample**

**PSDs calculated for Y and X data using  
Ewall parameters from Table 1**

**N<sub>2</sub> and Ar Adsorption Isotherms for Zeolite Y Sample**

**N2 and Ar Adsorption Isotherms for ZSM5 Sample**

**PSDs calculated for ZSM5 data using  
Ewall parameters from Table 1**